

## Handling of Time

### Central Pattern Generator

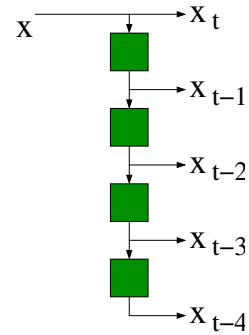
Neuronal circuit which produces rhythmic output

- Locomotion (walking, swimming, flying)
- Breathing
- Scratching
  
- Mutual inhibition
- Pacemaker cell properties

- 1 Central Pattern Generators
- 2 Feed-Forward Networks
  - Tapped Delay Line
  - Time Lagged Feed-Forward Networks
- 3 Recurrent Networks
  - Different Architectures
  - Finite-State Machines
- 4 Training of Recurrent Networks
  - Back-Propagation Through Time

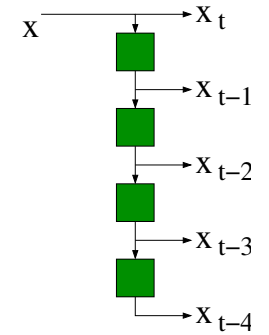
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- Temporal signals are tricky
- Transform temporal signals to spatial
- Tapped Delay Line

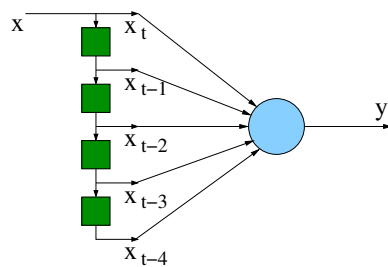


Design choices

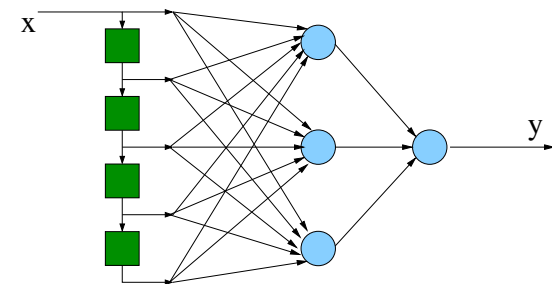
- Memory depth  
Number of time-steps saved
- Resolution  
Size of time-steps



Simplest form: "Neuronal filter"

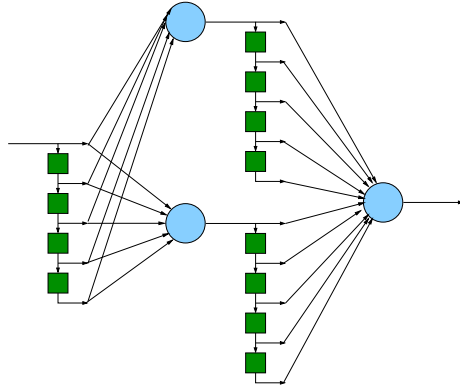


Multi-Layer Network



Delay of **all** signals

- More general
- Harder to train



How can we train a network with delays?

- Ordinary Back-Prop?
- Works when only the input is delayed
- Generalizations are needed when general delays are included
- The error signal must be matched against **old** activity values

1 Central Pattern Generators

2 Feed-Forward Networks

- Tapped Delay Line
- Time Lagged Feed-Forward Networks

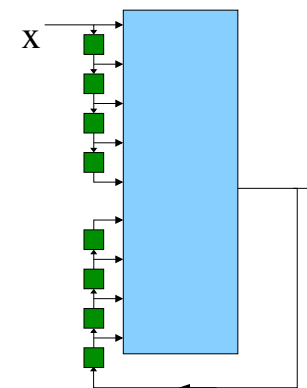
3 Recurrent Networks

- Different Architectures
- Finite-State Machines

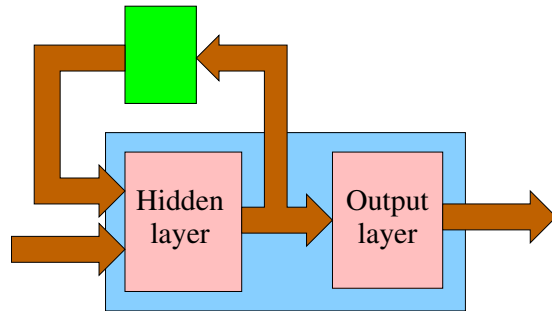
4 Training of Recurrent Networks

- Back-Propagation Through Time

Feedback of the output



Feedback from the hidden layer in next time-step

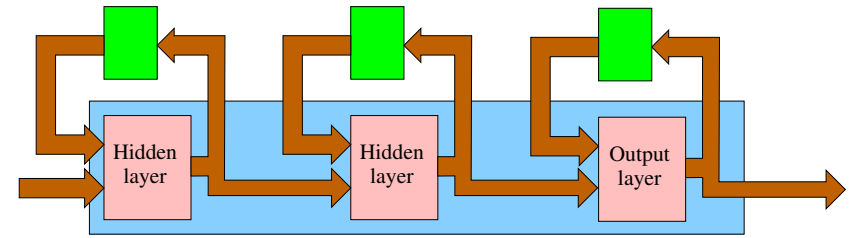


Context Units

Second Order Networks

- Product of input signal and feedback
- Every pair:  $\langle \text{in-signal} \times \text{feedback} \rangle$  has its own weight
- Many (specific) weights

Multi-Layered Recurrent Network

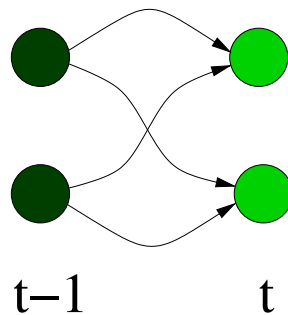
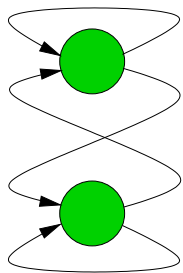


What can a recurrent network do?

- Finite-State Machine
- State corresponds to activity in the context nodes
- Combination of state and input produces next state

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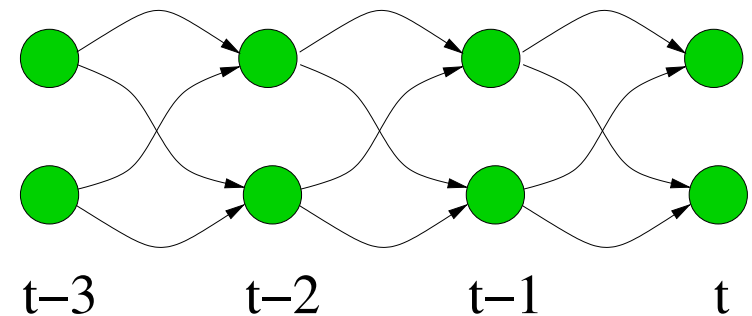
- Recurrent network with delayed connections
- Current state depends (only) on the previous state

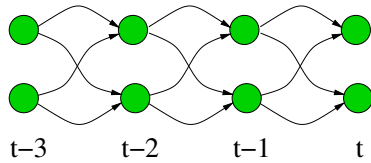


Is it possible to train a recurrent network to reproduce given sequences?

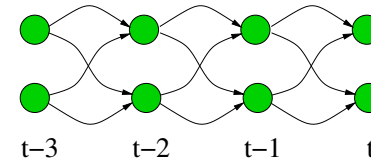
- Back-Propagation Through Time

Unfolding of the History





- Back-Propagation Through Time
- Target values are spread out over different layers
- Add contributions from all goals
- The same weight occurs in multiple places!
- Add contribution from all places



- All old activity values must be stored
- Problematic when learning long sequences
- Truncation of the history