

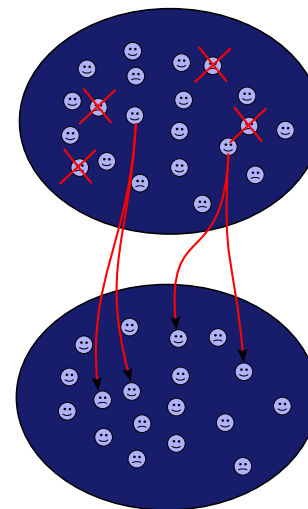
Genetic Algorithms

Genetic Algorithms

Parallel optimization inspired by biological evolution

- Populations of Hypotheses
- Selection Process
- Local Variation

- 1 Foundations
- 2 Algorithm Components
 - Coding of Hypotheses
 - Fitness Functions
 - Selection
 - Variation
- 3 Numerical Optimization
- 4 Genetic Programming
 - Example



- Population of **Individuals**
- **Selection** of the best individuals
- **Variation** creates new individuals
- New **Generations** created iteratively

1 Foundations

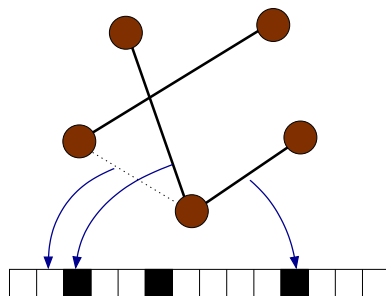
- 2 **Algorithm Components**
- Coding of Hypotheses
 - Fitness Functions
 - Selection
 - Variation

3 Numerical Optimization

- 4 **Genetic Programming**
- Example

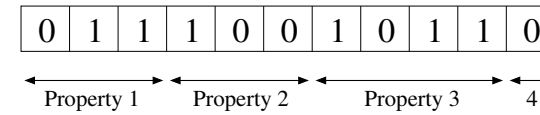
Example: Optimal choice of edges in a graph

The edges are encoded as a bit string



How are different hypotheses stored?

Chromosomes — Binary Strings



- **Genotype**
 The actual representation (the chromosome)
- **Phenotype**
 Properties of the individual (interpretation)

Do we *have* to use bit strings?

Variants:

- Other integers than only 0/1
- Real numbers
- Variable length
- Tree structures

Fitness Function

Measure of how good the hypothesis is

$$f : \text{chromosome} \mapsto \mathcal{R}$$

Example:

- Total path length in a graph
- Error in a function approximation
- Performance of a simulated robot
- Number of games won

Evaluating the fitness functions is normally the *most time consuming* part of a genetic algorithm

Variation

- **Mutations**
Small random modifications
- **Crossovers**
Mixing of individuals content

Selection

Basic idea: Preserve individuals with a high fitness

- **Roulette selection**
Probability of survival proportional to f
- **Ranking selection**
Selection based on order instead of the actual fitness value
- **Tournament selection**
Random pairs are formed and the one with highest fitness survives
- **Elitism**
The best individuals in a generation are guaranteed to survive

Mutations

- Make random changes to the contents of the chromosome
- Choice of coding makes a big difference

Crossovers

- Select two individuals with high fitness
- Exchange parts of the chromosome with each other

One-point crossover

Multi-point crossover

Example: Optimized code generation from a compiler

ACOVEA — Analysis of Compiler Options via Evolutionary Algorithms

Software for finding the optimal compiler options for a given C program

Application on ordinary optimization problems

Assume that we are looking for $\max f(x, y)$

Encoding: chromosome consisting of two real numbers

Each individual corresponds to a point in the plane

- Mutations
Redistribution parallel to the x and y axis
- Crossovers
New points with x from one parent and y from the other

Genetic Programming

The use of GA to automatically create programs

- How are programs represented?
- How can one measure fitness?
- How are mutations done?
- How are crossovers done?

Representation of Programs

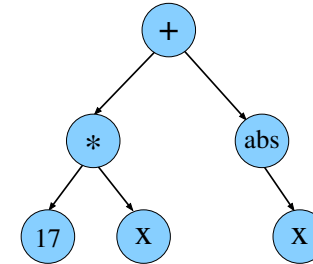
Ordinary programming languages are not suitable

- Tree with operators
- List of instructions

Example

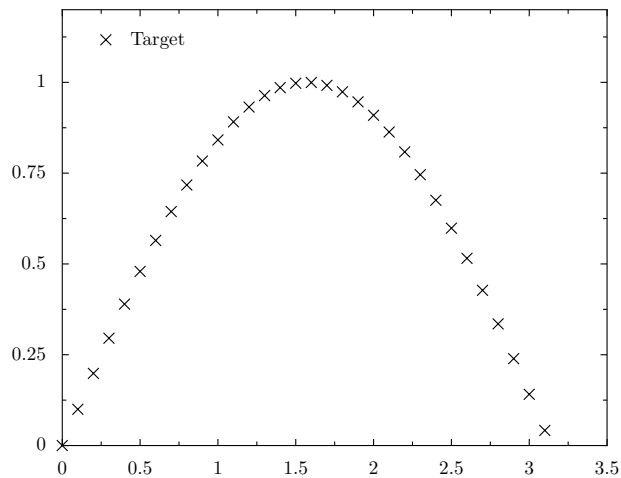
Function Approximation

Representation of the program

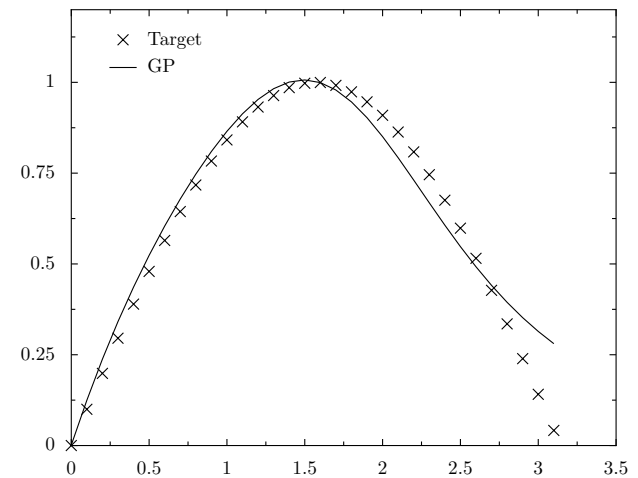


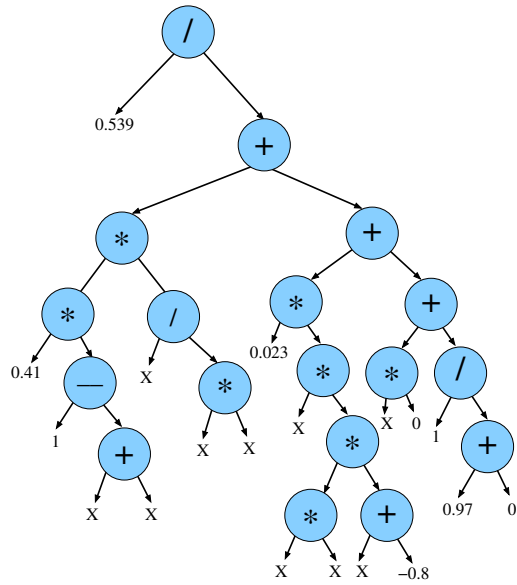
- Mutations
- Crossovers

Goal Function



Solution found by the algorithm





Bloating

Accumulation of unnecessary parts in chromosomes with variable length