# Evaluating Functions 

## and Conditionals

7 September 2022

Assignment 1 due 11:59pm on Wednesday
Assignment 2 comes out on Thursday

Where are we?

## We've been using Pyret to write expressions that

 use:Data, including

```
numbers (0, -10, 0.4),
strings ("", "hi", "111"), and
images (circle(2, "solid", "red")).
```

Which we modify or combine using operators or functions like +, string-append, and above.

Distinguishing types of data helps to catch mistakes.

If you try to give
a string to / or
a number to overlay,
we want Pyret to catch the problem right early, giving a helpful error message.

We've seen that we can create more complicated programs by composing function calls, e.g.,

$$
1+(2 / 3)
$$

or

```
string-append("hello ",
    string-append("Pyret ", "world!"))
```

And we can give a name to the result of an expression, e.g.,

$$
\operatorname{total}=2+3
$$

Defining functions

Remember functions from middle-school math:
Given $f(x)=\cos (x)+2$

$$
f(0)=1+2=3
$$

Parameter stands for
varying value

Pyret functions work the same way:
fun $f(x):$ num-cos(x) +2 end
f(0)
$\rightarrow$ num- $\cos (0)+2$
$\rightarrow 1+2$
$\rightarrow 3$

Function definitions in Pyret have this form：
fun〈function－name〉（〈arg－name〉，．．．）：〈expression〉

Example

Mary Berry needs to know how many cakes to bake for her cake shop.

To avoid running out or having too many, she likes to bake two cakes more than the number she sold the previous day.
E.g., if Mary sells eight cakes on Monday, she makes ten cakes on Tuesday.
Let's write some code to help Mary.


end
end

fun cakes-to-make(num-sold): num-sold + 2
end

fun cakes-to-make(num-sold): num-sold + 2


Functional abstraction
\# Draw a traffic light
above( circle(40, "solid", "red"), above ( $\begin{gathered}\text { circle(40, "solid", } \\ \text { circle(40, "solid", }\end{gathered}$ "yellow") "green"))
Unchanging

Varying

```
# Draw a traffic light
above(circle(40, "solid", "red"),
    above(circle(40, "solid", "yellow"),
        circle(40, "solid", "green")))
# Can be changed to
fun bulb(color):
    circle(40, "solid", color)
end
above(bulb("red"),
    above(bulb("yellow"),
        bulb("green")))
```

fun bulb(color): circle(40, "solid", color) end
fun traffic-light(): above(bulb("red"), above(bulb("yellow"), bulb("green")))
end

Example

For Mary's cake shop, we want to determine the price of each cake based on the cost of the ingredients and the time to prepare it.

The price is twice the cost of the ingredients plus $1 / 4$ of the preparation time in minutes.

Chocolate cake Ingredients: \$10
Preparation time: 20 minutes

Cheesecake
Ingredients: \$15
Preparation time: 36 minutes

$$
\text { choc-cake-price }=(2 * 10)+(0.25 * 20)
$$

We use functions to
avoid repetitive code when we need to perform the same operations on different values.
choc-cake-price $=(2 * 10)+(0.25 * 20)$
cheesecake-price $=(2 * 15)+(0.25 * 36)$

$$
(2 * \text { ingredients-cost })+(0.25 * \text { prep-time })
$$

We use functions to
avoid repetitive code
when we need to
perform the same
operations on different
values.

$$
\text { choc-cake-price }=(2 * 10)+(0.25 * 20)
$$

$$
\text { cheesecake-price }=(2 *(15)+(0.25 * 36)
$$



The parameters are the values passed into the function
that it needs to know for each operation.
fun cake-price(ingredients-cost, prep-time): (2 * ingredients-cost) $+(0.25 *$ prep-time)

Expression repeated each time the function is called

## fun cake-price(ingredients-cost, prep-time):

```
(2 * ingredients-cost) + (0.25 * prep-time)
```

end

```
To calculate the price of chocolate cake or cheesecake, you
simply call your function and pass in the relevant values:
```

```
# Price of chocolate cake
cake-price(10, 20)
```

\# Price of cheesecake
cake-price(15, 36)

## Improving our function definitions

```
fun cake-price(ingredients-cost :: Number,
    prep-time :: Number):
    (2 * ingredients-cost) + (0.25 * prep-time)
```

We specify the type of each parameter so that Pyret will check that we pass in the right kind of values, just like for built-in operations like + and above.

```
fun cake-price(ingredients-cost :: Number,
    prep-time :: Number) -> Number:
    (2 * ingredients-cost) + (0.25 * prep-time)
```

And we can specify the type of value the function returns.

| -००<> $\square$ code.pyret.org/editor |  |
| :---: | :---: |
| - - View Connect to Google Drive | Run $\quad \square$ Stop |
| ```use context essentials2021 fun cake-price(ingredients-cost :: Number, prep-time :: Number) -> Number: (2 * ingredients-cost) + (0.25 * prep-time) end``` | "'cake-price(2, 3) <br> 4.75 <br> "'cake-price("banana", "bundt") <br> The Number annotation $\qquad$ |

```
fun cake-price(ingredients-cost :: Number,
    prep-time :: Number) -> Number:
    doc: "Calculate price of cake based on
ingredient cost and prep time"
    (2 * ingredients-cost) + (0.25 * prep-time)
```

Additionally, a docstring explains what the function does.
"Programs must be written for people to read, and only incidentally for machines to execute."

Hal Abelson \& Gerald Sussman with Julie Sussman, Structure and Interpretation of Computer Programs, 1979
fun cakes-to-make(num-sold :: Number) -> Number:
doc: "Compute the number of cakes to make based on the previous number sold" num-sold + 2
end
fun cakes-to-make(num-sold :: Number) -> Number:
doc: "Compute the number of cakes to make based on the previous number sold"
num-sold +2
where:
cakes-to-make(0) is 2
cakes-to-make(107) is 109
end



fun rectangle-area(r): image-height(r) * image-width(r) end
fun rectangle-area(r :: Image) $\rightarrow$ Number:
doc: "Return the rectangular area of the image"
image-height(r) * image-width(r)
where:
rectangle-area(rectangle(0, 0, "solid", "black")) is 0
rectangle-area(rectangle(2, 3, "outline", "blue")) is 6
end

## Booleans and if expressions

true
false

To combine Boolean values，we can use and：
〈expression 1〉 and 〈expression 2〉
and or：
〈expression 1〉 or 〈expression 2〉
Evaluation of and stops－is＂short－circuited＂－as
soon as one of the expressions being combined evaluates to false．

Evaluation of or stops as soon as one of the expressions evaluates to true．
>> true and false
false
>>> true or false
true
>>> $(\mathbf{1}<\mathbf{2})$ and $(2>3)$
false
〉> $(1<=0)$ or ( $1==1)$
true

To change an expression that evaluates to true to be false or vice versa, use not:

$$
\begin{aligned}
& \text { ") } \\
& \text { true }
\end{aligned}
$$

```
i1 = rectangle(10, 20, "solid", "red")
i2 = rectangle(20, 10, "solid", "blue")
```

image-width(i1) < image-width(i2)

```
rect = rectangle(10, 20, "solid"", "red"')
if image-width(rect) < image-height(rect):
    "tall"
else:
    "wide"
end
```



## Evaluation rule for if expressions

1 If the question expression is not a value, evaluate it, and replace with value.

2 If the question is true, replace entire if expression with true answer expression.

3 If the question is false, replace entire if expression with false answer expression.

4 If the question is a value other than true or false, so produce an error.

```
rect = rectangle(10, 20, "solid"", "red"')
if image-width(rect) < image-height(rect):
    "tall"
else:
    "wide"
end
```

What if, instead of producing a Boolean to say if an image is tall or not, we classify them as "tall", "square", or "wide"?
rect = rectangle(10, 20, "solid", "red")
if image-width(rect) < image-height(rect): "tall"
else if image-width(rect) == image-height(rect):
"square"
else:
"wide"
end

```
rect = rectangle(10, 20, "solid", "red")
fun image-type(img :: Image) -> String:
    doc: "Classify an image as tall, square, or wide"
    if image-width(img) < image-height(img):
        "tall"
    else if image-width(img) == image-height(img):
        "square"
    else:
        "wide"
    end
where:
    image-type(rect) is "tall"
end
```

```
rect = rectangle(10, 20, "solid", "red")
fun image-type(img :: Image) -> String:
    doc: "Classify an image as tall, square, or wide"
    if image-width(img) < image-height(img):
        "tall"
    else if image-width(img) == image-height(img):
        "square"
    else:
        "wide"
    end
where:
    image-type(rect) is "tall"
    image-type(rectangle(10, 10, "solid", "blue")) is "square"
    image-type(rectangle(20, 10, "solid", "blue")) is "wide"
end
```


## Acknowledgments

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