

Trees

Joyce Kilmer - 1886-1918

I think that I shall never see
A poem lovely as a tree.

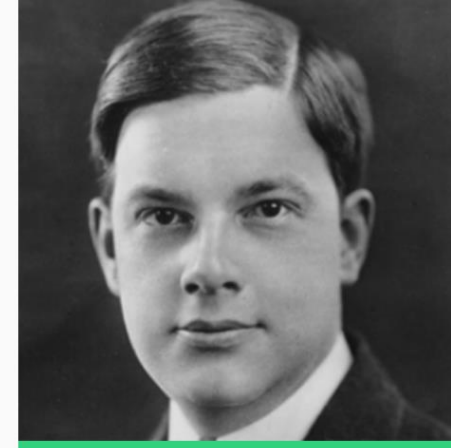
A tree whose hungry mouth is prest
Against the earth's sweet flowing breast;

A tree that looks at God all day,
And lifts her leafy arms to pray;

A tree that may in summer wear
A nest of robins in her hair;

Upon whose bosom snow has lain;
Who intimately lives with rain.

Poems are made by fools like me,
But only God can make a tree.



Joyce Kilmer was born on December 6, 1886, in New Brunswick, New Jersey. The author of *Main Street and Other Poems* (George H. Doran Company, 1917), he was killed while fighting in World War I.

Themes

nature

plants

[About Joyce Kilmer >](#)



Steps to write a generic template

- Given a (recursive) *data definition*, you write a generic template by:
 1. Creating a function header,
 2. Using *cases* to break the data input into its variants,
 - In each case, list each of the fields as part of the answer
 3. And, calling the function itself on any recursive fields.



Data Definition: Start With A Template

```
data MyList:  
  | my-empty  
  | my-link(first, rest :: MyList)  
end
```

Self-reference Definition!

Debrief: lists and recursion



```
data MyList:  
  | my-empty  
  | my-link(first, rest :: MyList)  
end
```

```
my-empty  
my-link(1,  
  my-link(2,  
    my-link(3,  
      my-empty)))
```

What's different here?

1. We have a case that's just a **special keyword** rather than a constructor.
2. Part of the second case" is of the same type we're defining.
 - **A recursive definition!**

Using my-list Data Template



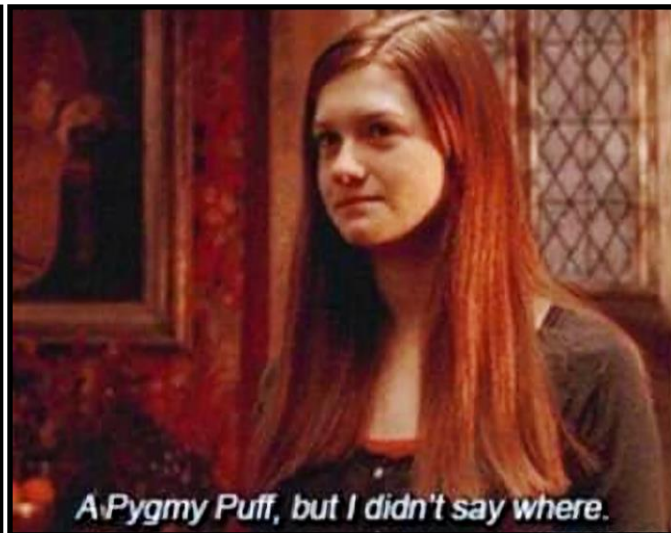
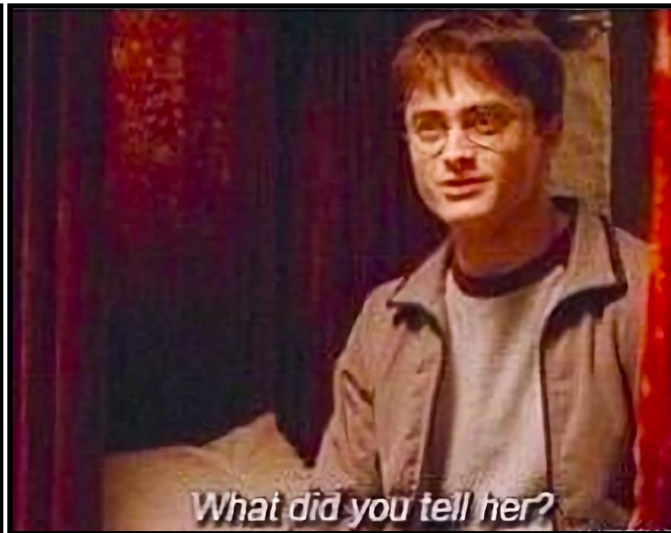
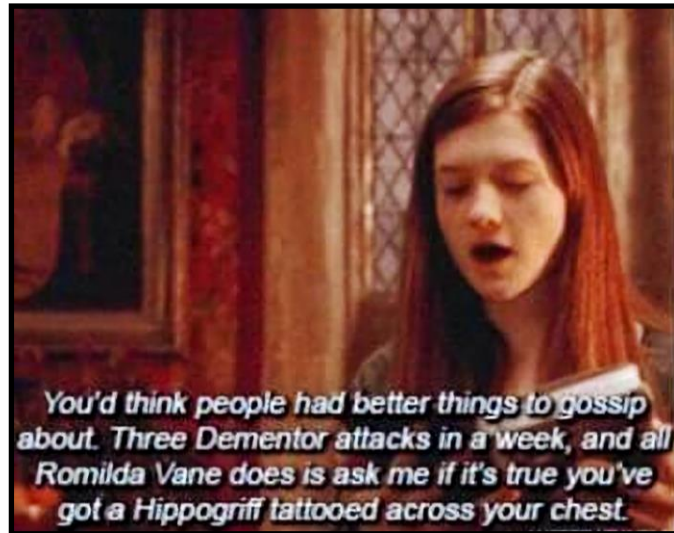
We use this template to write a function that recursively processes the data:

```
fun my-fun(ml :: MyList) -> ...:  
  doc: "Template for a function that takes a MyList"  
  cases (MyList) ml:  
    | my-empty => ...  
    | my-link(f, r) =>  
      ... f ...  
      ... my-fun(r) ...  
  end  
where:  
  my-fun(...) is ...  
end
```

Tracking rumors



- Suppose we want to track gossip in a rumor mill.



Ginny controls the rumor mill

Tracking rumors



- Suppose we want to track gossip in a rumor mill.



Pansy

Tracking rumors



- Suppose we want to track gossip in a rumor mill.

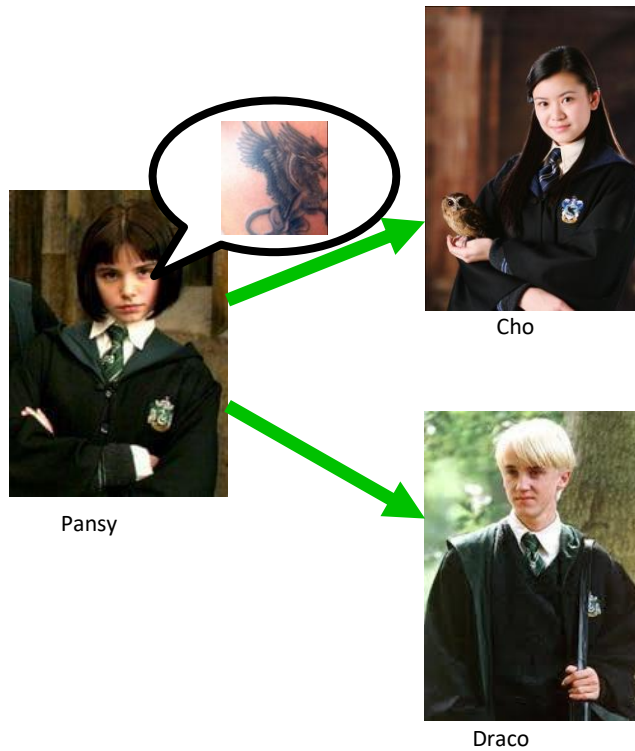


Pansy

Tracking rumors



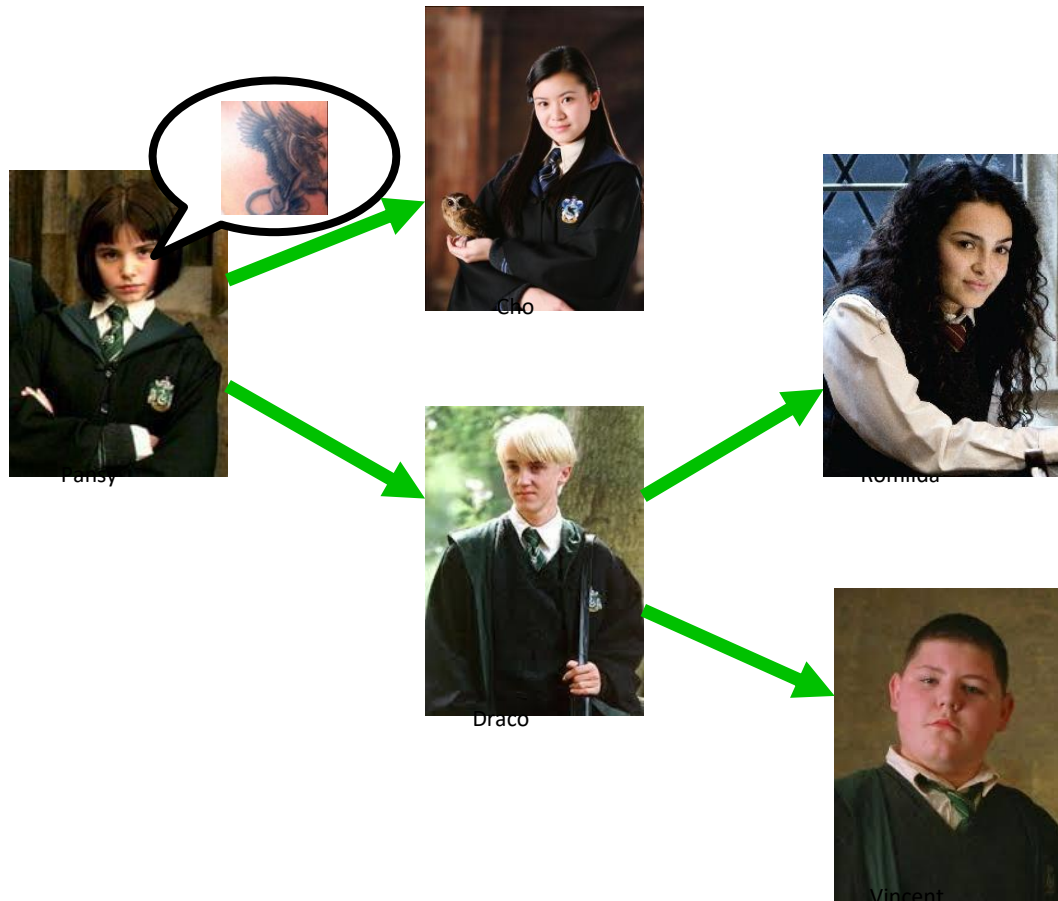
- Suppose we want to track gossip in a rumor mill.



Tracking rumors



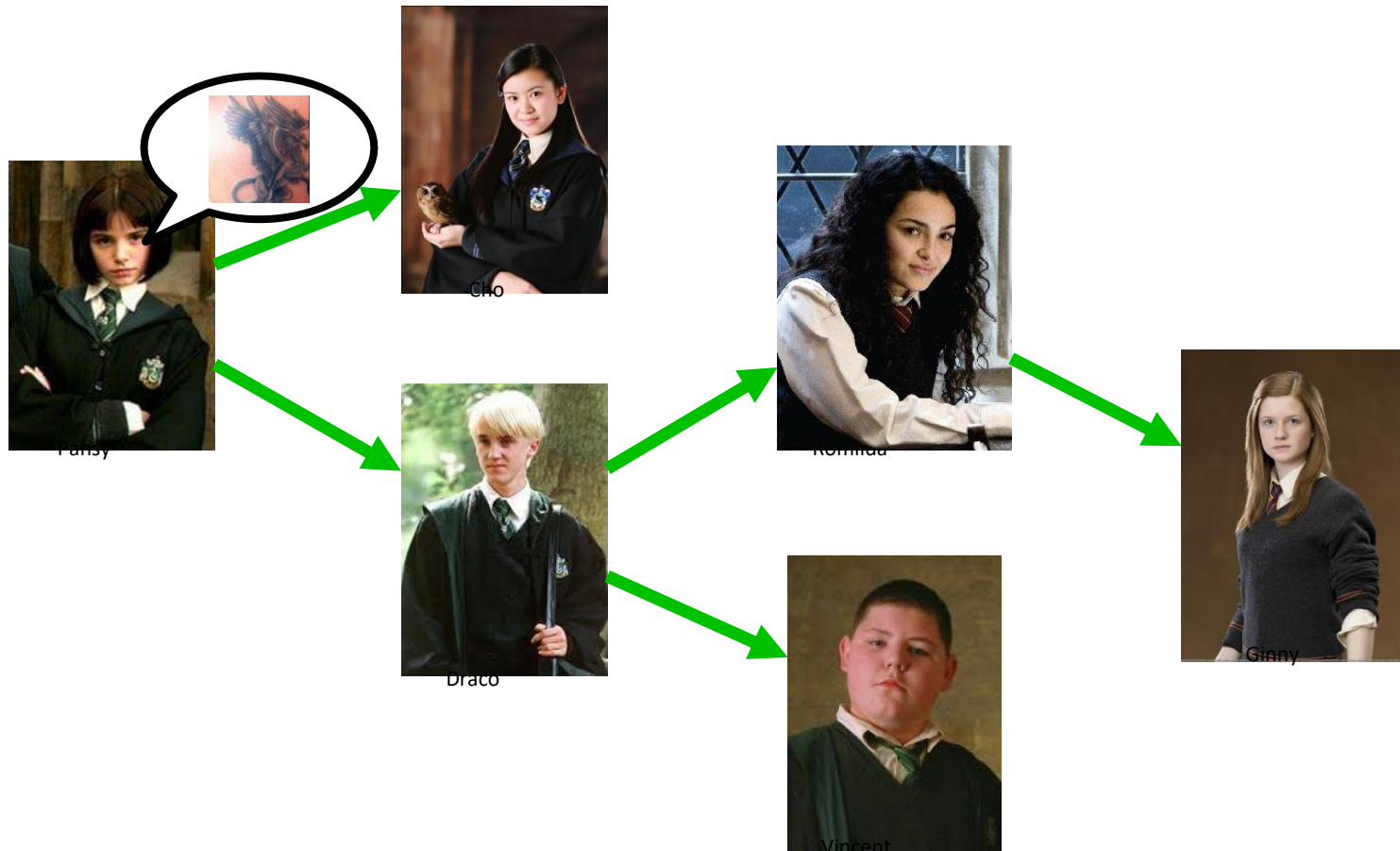
- Suppose we want to track gossip in a rumor mill.



Tracking rumors



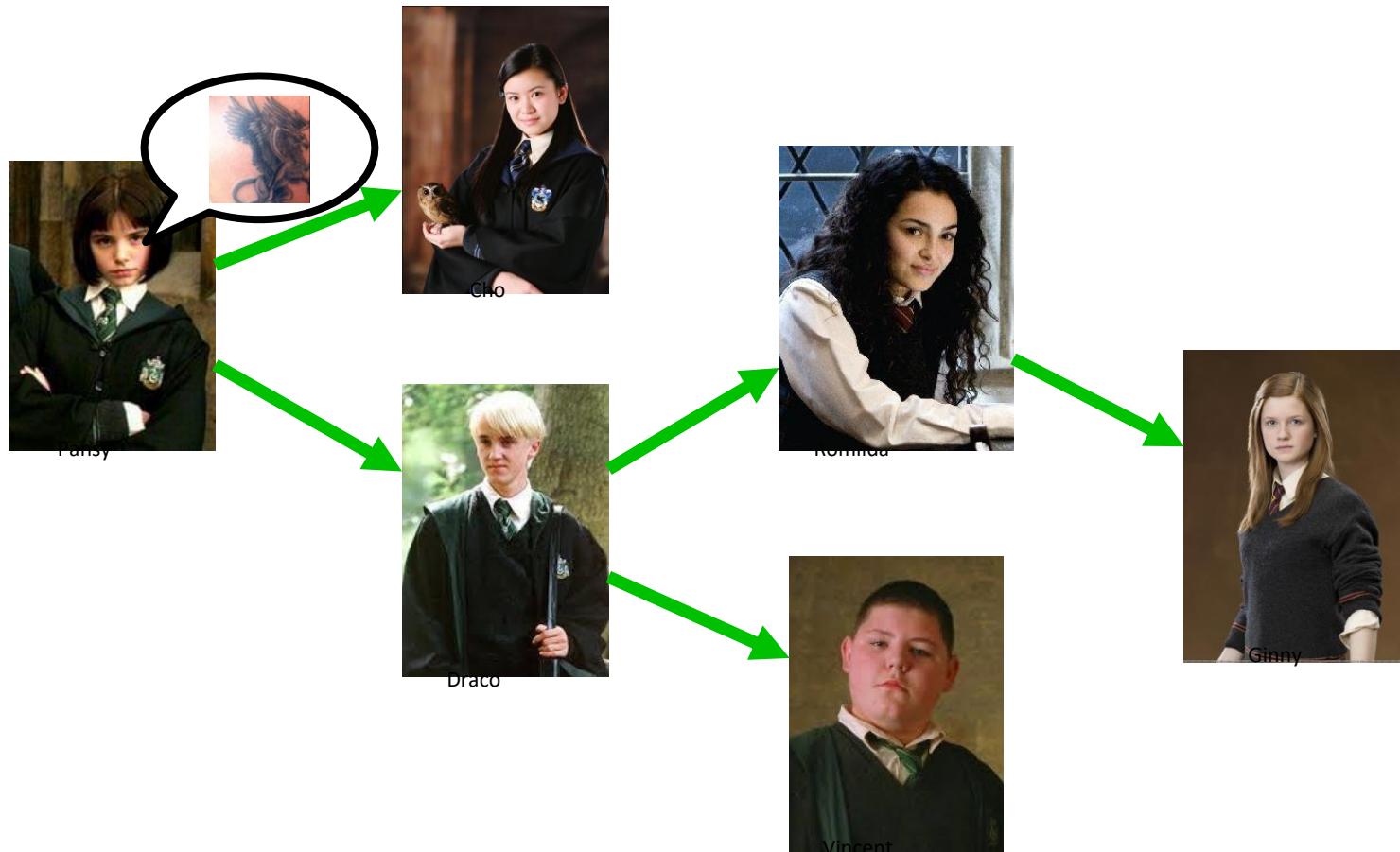
- Suppose we want to track gossip in a rumor mill.



Tracking rumors



- Suppose we want to track gossip in a rumor mill.

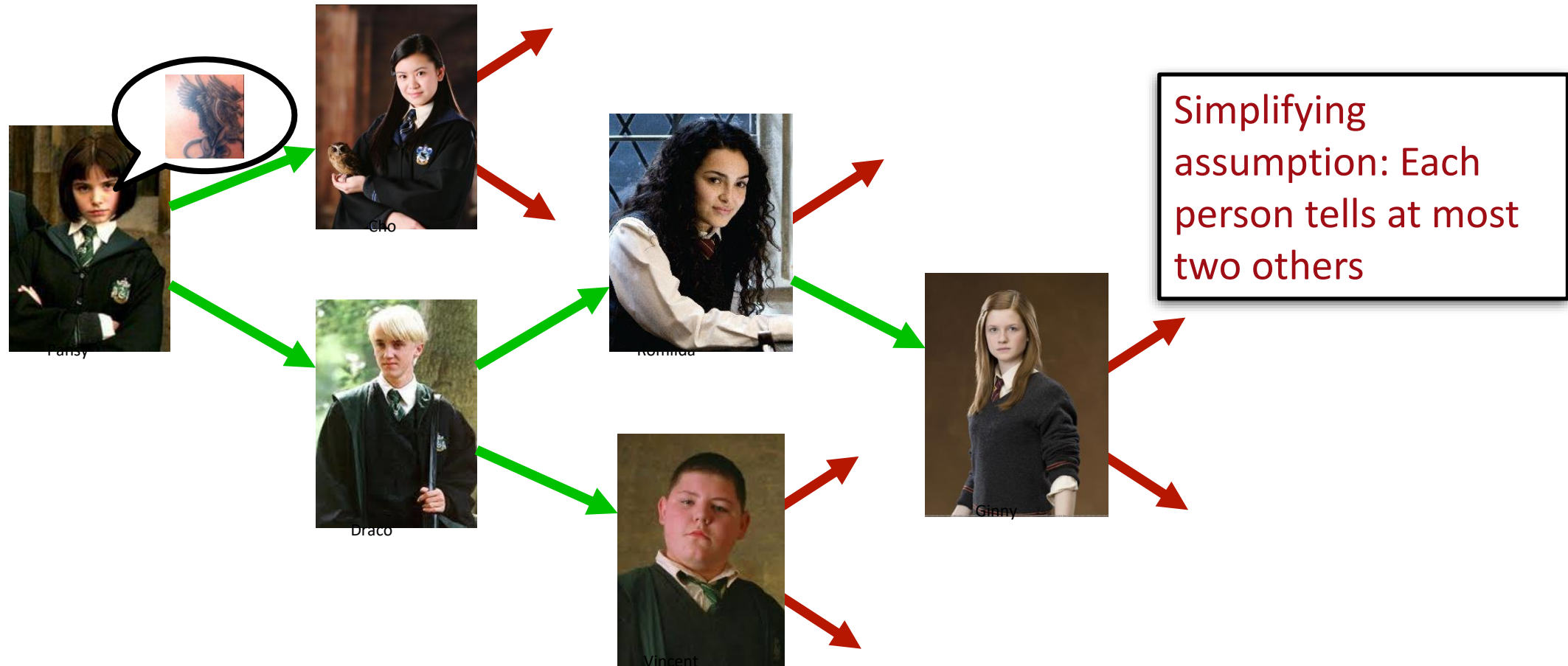


Simplifying assumption: Each person tells at most two others

Tracking rumors



- Suppose we want to track gossip in a rumor mill.



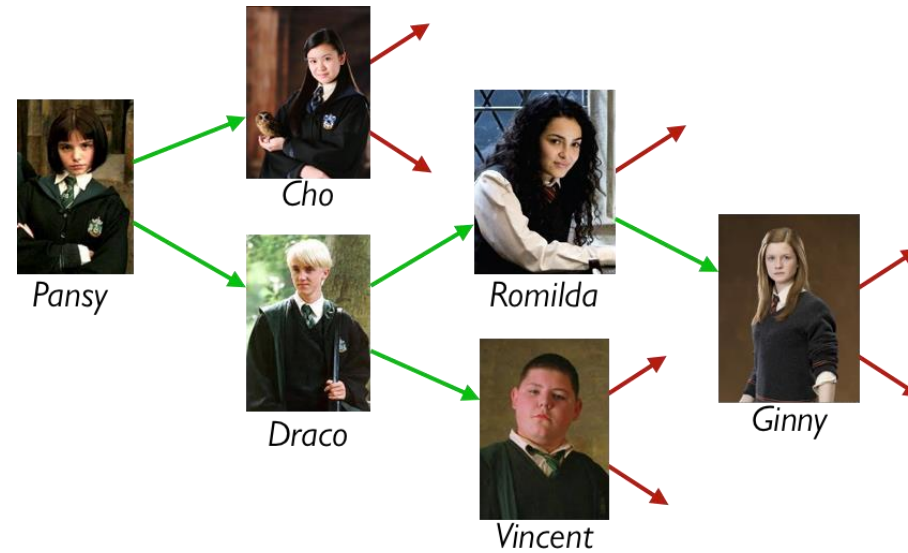
Tracking rumors



- If you ignore my silly Harry Potter example, this is a pretty serious problem.
- A lot of research right now is focused on building models of how information – and misinformation! – spreads through social networks, both in person and online.



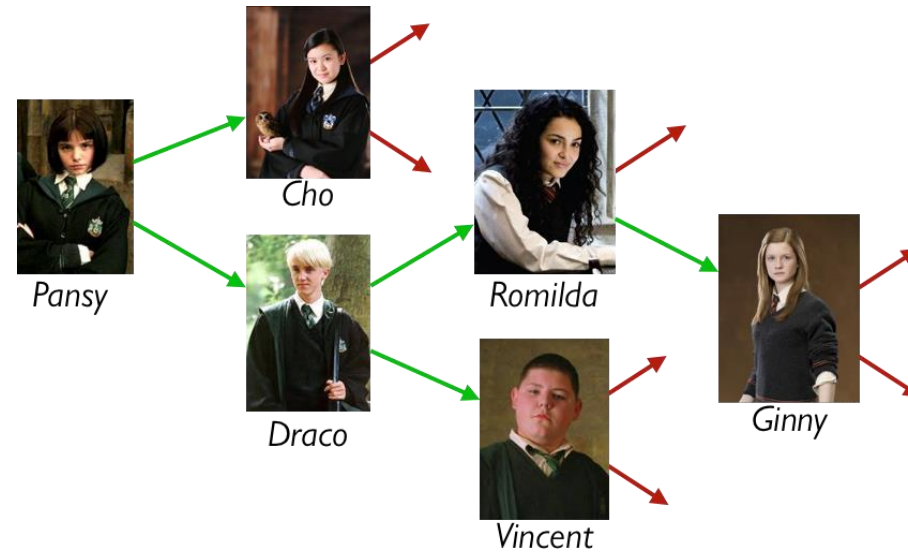
Representing rumor mills



Is a rumor mill simply a list of people?



Representing rumor mills

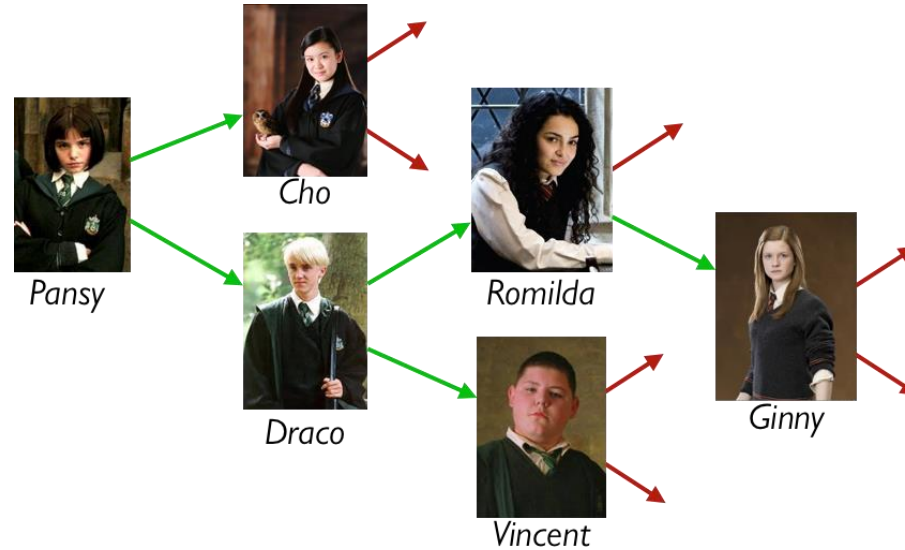


Question: Is a rumor mill simply a list of people?

Answer: No, because there are *relationships* among the people.



Representing rumor mills



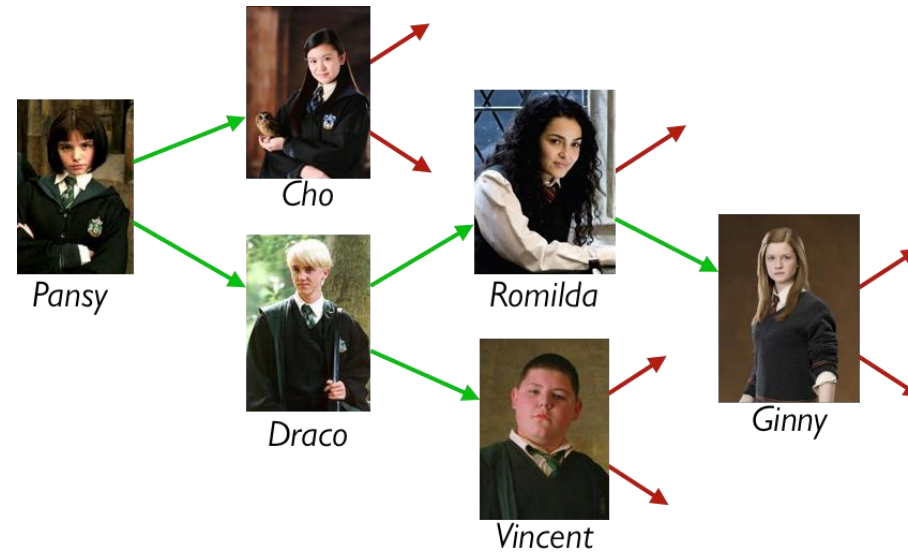
We *could* represent these

relations with a table, e.g.,

<code>name :: String</code>	<code>next1 :: String</code>	<code>next2 :: String</code>
"Pansy"	"Cho"	"Draco"
"Cho"		
...



Representing rumor mills

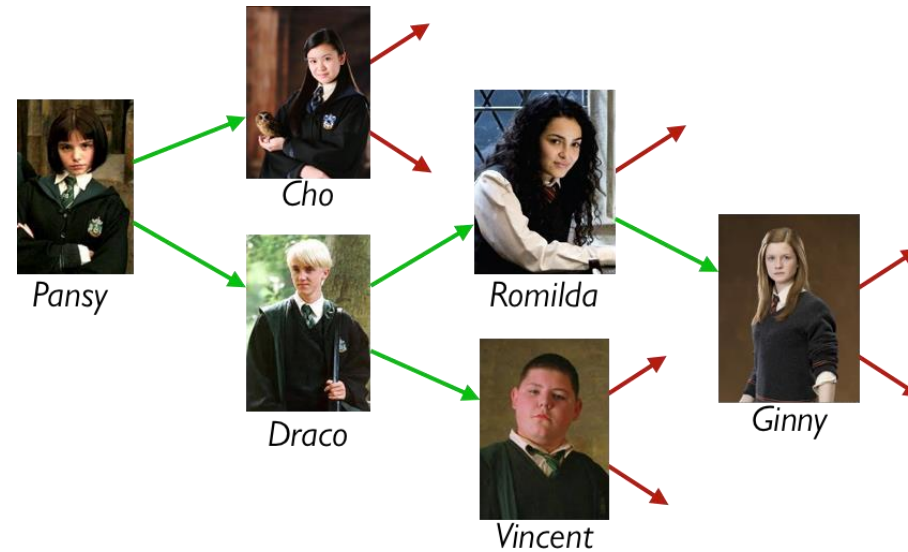


Using a table doesn't give us any straightforward way to process the rumor mill.

Could we use something *like* a list but representing the relations?



Representing rumor mills



data **Person**:

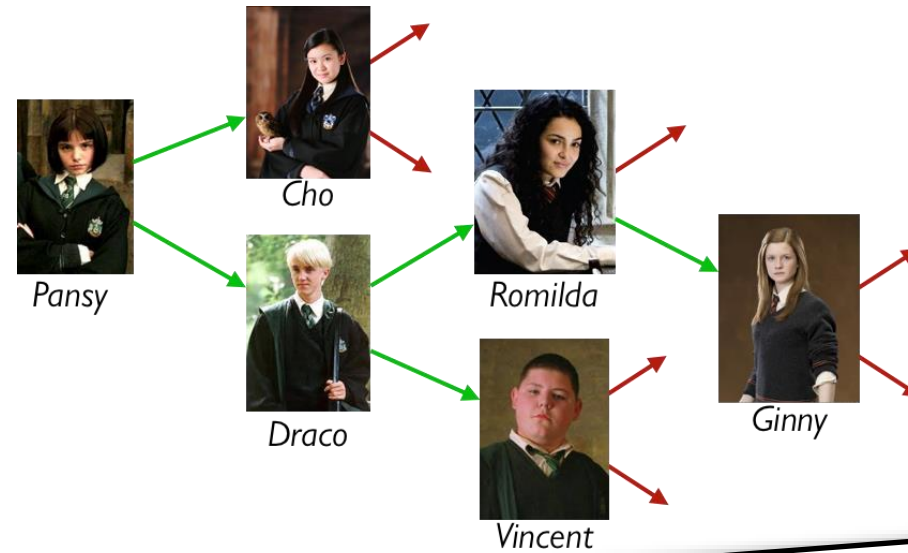
```
| person(name :: String, next1 :: Person, next2 :: Person)
```

```
end
```

How about this?



Representing rumor mills



Some people don't gossip to anyone else – see the red arrows above.

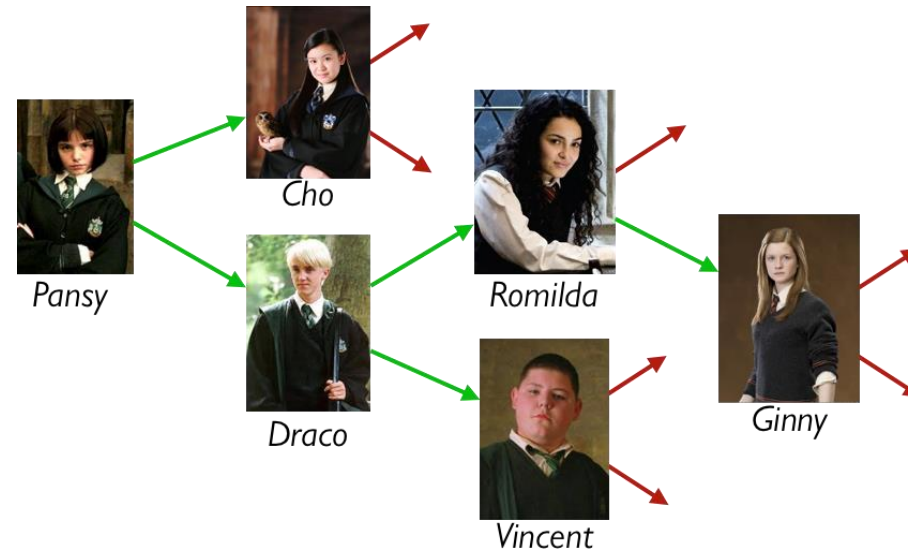
data **Person**:

```
| person(name :: String, next1 :: Person, next2 :: Person)
```

```
end
```



Representing rumor mills



data **RumorMill**:

| no-one

| gossip(name :: String, next1 :: RumorMill, next2 :: RumorMill)

end

How about this?



Example rumor mills

```
data RumorMill:  
  | no-one #at the start there is... no-one in the rumor mill!  
  | gossip(name :: String, next1 :: RumorMill, next2 :: RumorMill)  
end
```

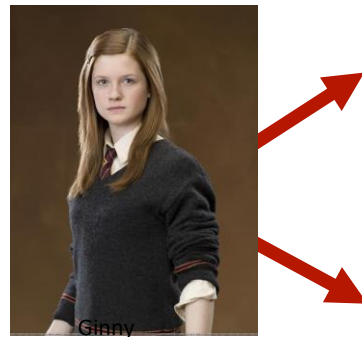
no-one



Example rumor mills

```
data RumorMill:  
  | no-one  
  | gossip(name :: String, next1 :: RumorMill, next2 :: RumorMill)  
end
```

```
gossip("Ginny", no-one, no-one)
```





Example rumor mills

```
data RumorMill:  
  | no-one  
  | gossip(name :: String, next1 :: RumorMill, next2 :: RumorMill)  
end
```

```
gossip("Romilda",  
  no-one,  
  gossip("Ginny", no-one, no-one))
```



Romilda

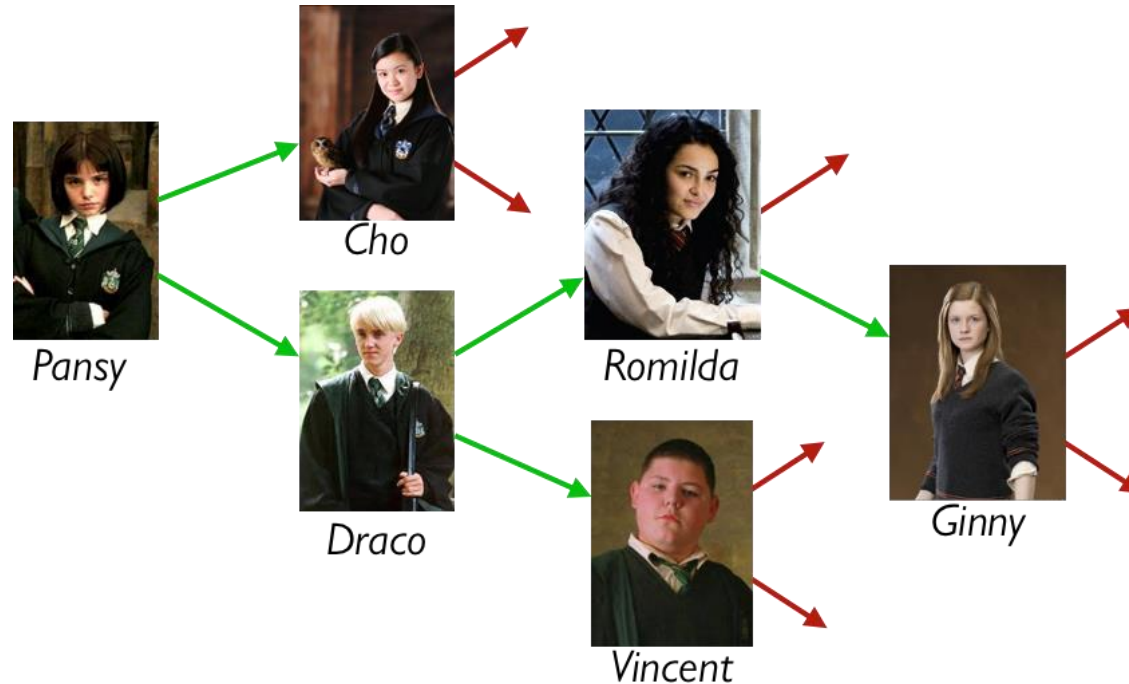


Ginny





```
gossip("Pansy",  
      gossip("Cho", no-one, no-one)  
      gossip("Draco",  
            gossip("Romilda",  
                  no-one  
                  gossip("Ginny", no-one, no-one))  
            gossip("Vincent", no-one, no-one)))
```



Example, using names for the parts



GINNY-MILL =

`gossip("Ginny", no-one, no-one)`

ROMILDA-MILL =

`gossip("Romilda", no-one, GINNY-MILL)`

VINCENT-MILL =

`gossip("Vincent", no-one, no-one)`

DRACO-MILL =

`gossip("Draco", ROMILDA-MILL, VINCENT-MILL)`

CHO-MILL =

`gossip("Cho", no-one, no-one)`

PANSY-MILL =

`gossip("Pansy", CHO-MILL, DRACO-MILL)`

Computer Science concepts wrung from a rumor mill



- A *RumorMill* is a type of structure called a *tree*.
 - Each element in the tree is called a *node*.
 - The first node in the tree is called the *root*.
 - A node with no children is called a *leaf*.
- Like a list, a tree is recursive: Every subtree is a tree.

Programming with rumors

```
data RumorMill:  
  | no-one  
  | gossip(name :: String, next1 :: RumorMill, next2 :: RumorMill)  
end
```

Self-reference × 2



For each element, there's not just one "next" element; there are two!

Rumor Mill Template

Programming with rumors

```
data RumorMill:  
  | no-one  
  | gossip(name :: String, next1 :: RumorMill, next2 :: RumorMill)  
end  
#|  
fun rumor-mill-template(rm :: RumorMill) -> ...:  
  doc: "Template for a function with a RumorMill as input"  
  cases (RumorMill) rm:  
    | no-one => ...  
    | gossip(name, n1, n2) =>  
      ... name  
      ... rumor-mill-template(n1)  
      ... rumor-mill-template(n2)  
  end  
end  
|#
```

Self-reference × 2



Rumor Mill Template



Programming with rumors

```
data RumorMill:  
  | no-one  
  | gossip(name :: String, next1 :: RumorMill, next2 :: RumorMill)  
end  
#|  
fun rumor-mill-template(rm :: RumorMill) -> ...:  
  doc: "Template for a function with a RumorMill as input"  
  cases (RumorMill) rm:  
    | no-one => ...  
    | gossip(name, n1, n2) =>  
      ... name  
      ... rumor-mill-template(n1)
```

Self-reference × 2

Natural recursion × 2



Link to code

- [14-new-data-types.arr](#)

Acknowledgements



- This lecture incorporates material from:
- Kathi Fisler, Brown University,
- Marc Smith, Vassar College
- And, Jonathan Gordon, Vassar College