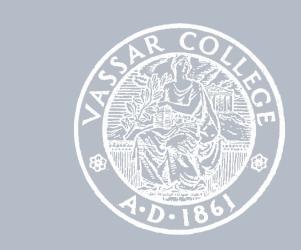
CMPU 366 · Natural Language Processing

Large Language Models

Part 2

29 October 2025



Where are we?

A *language model* gives the probability for the next token given some prefix: $P(w_i \mid w_{< i})$

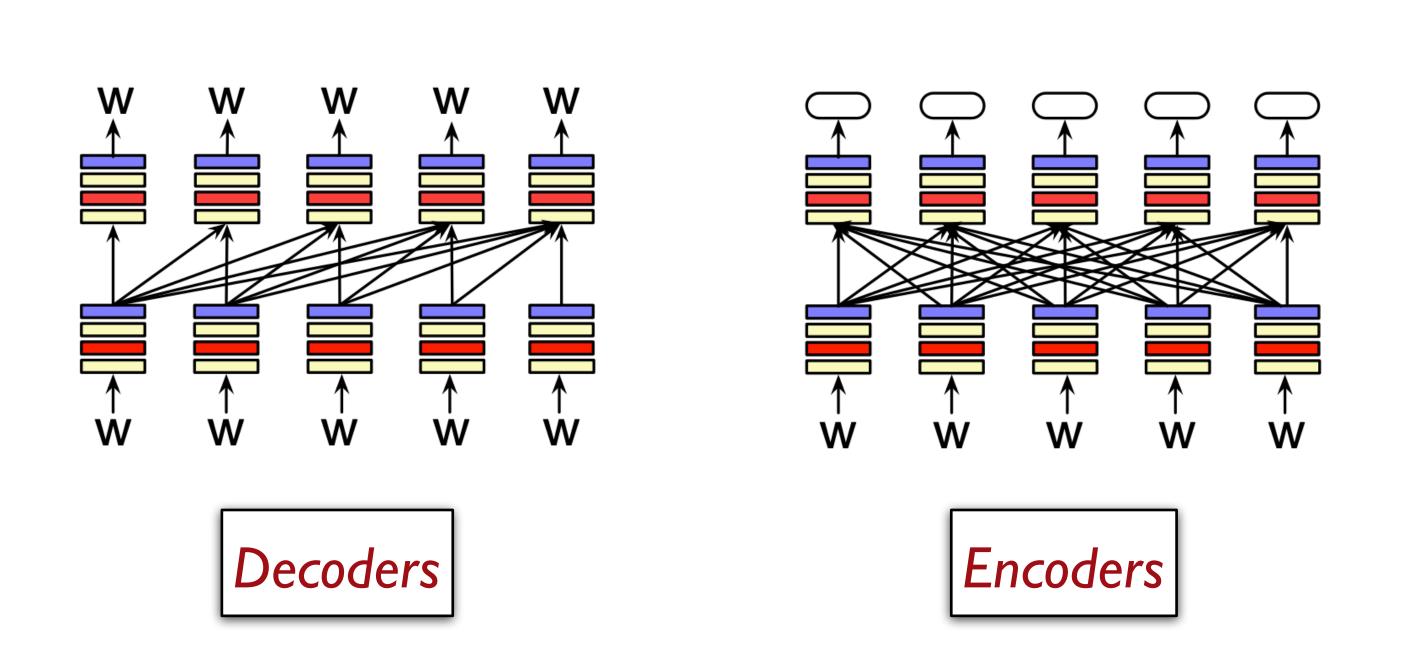
Using these probabilities, we can also compute the probability of an entire sequence of tokens (using the chain rule) – or to generate new text.

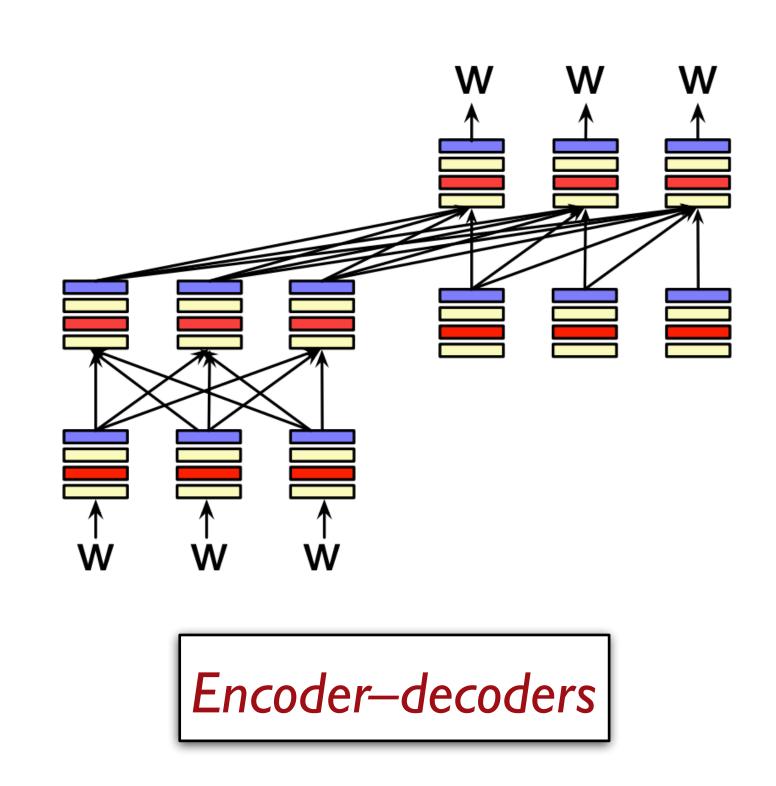
A large language model is distinguished from traditional language models by

the use of neural networks to learn to predict the next word given a variable-length context rather than counting words seen after a fixed-length prefix and

the ("large") number of parameters in the network.

Three architectures for LLMs





Text generation using LLMs depends on the choice of decoding method:

greedy decoding or

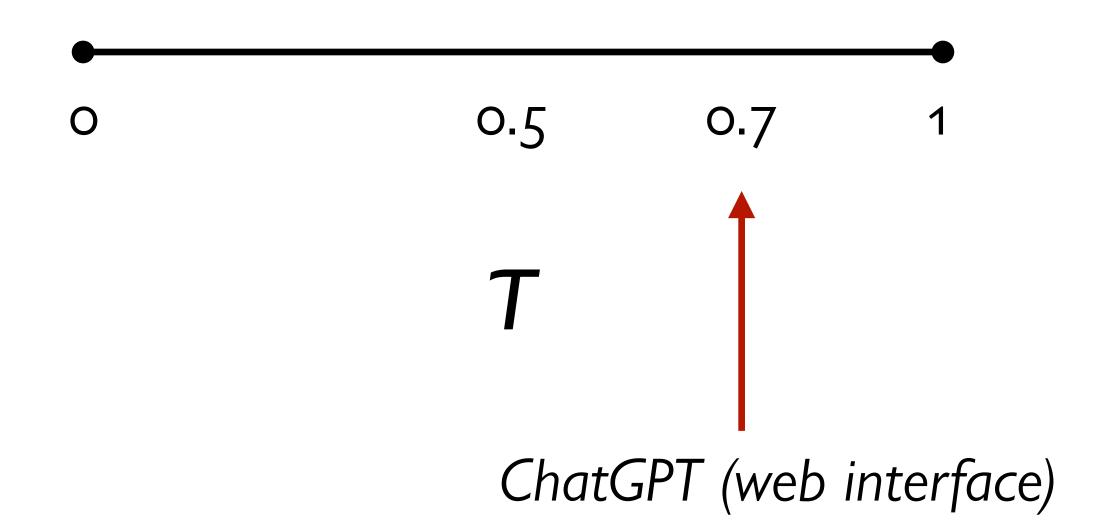
sampling.

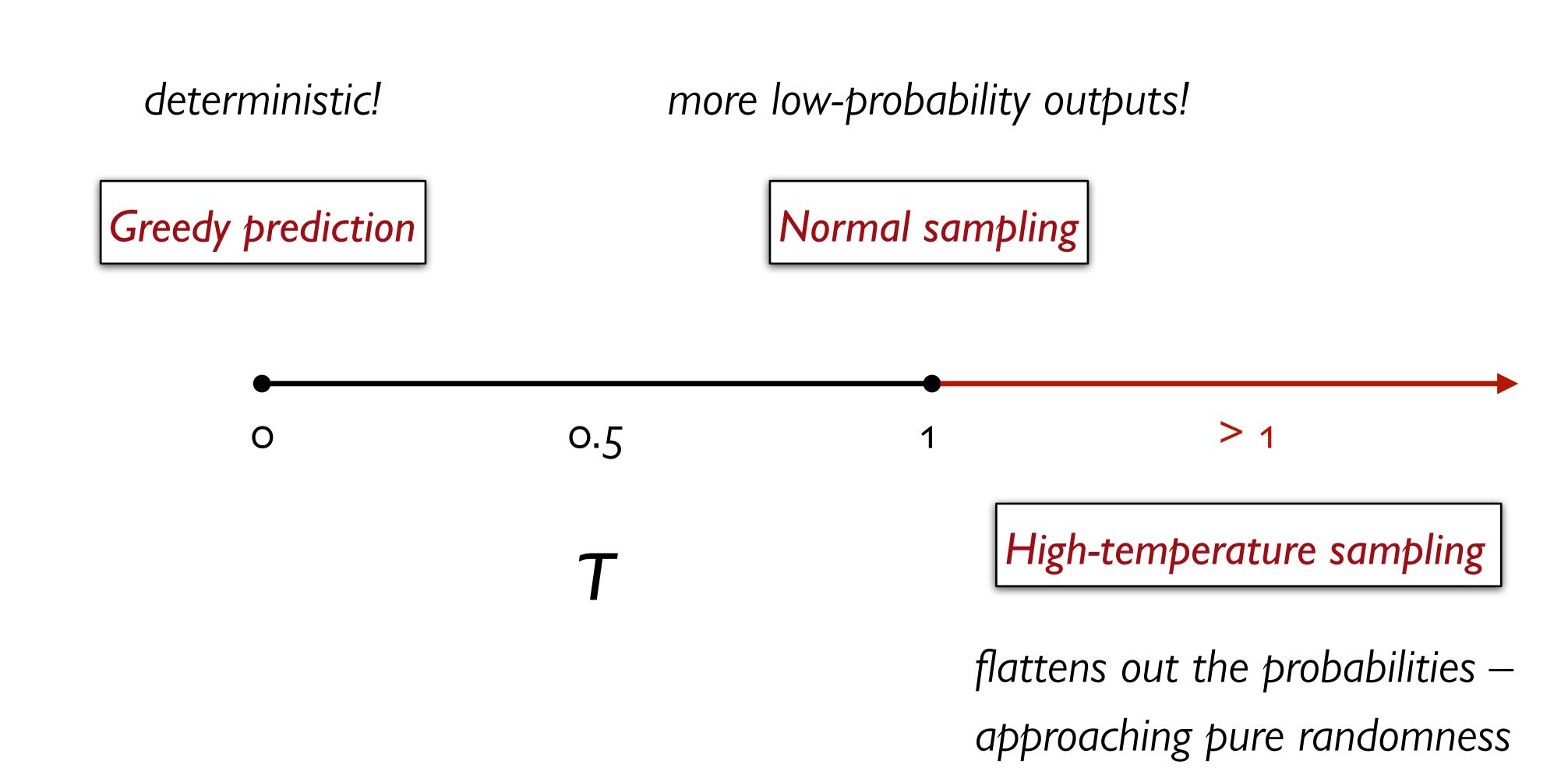
deterministic!

more low-probability outputs!

Greedy prediction

Normal sampling

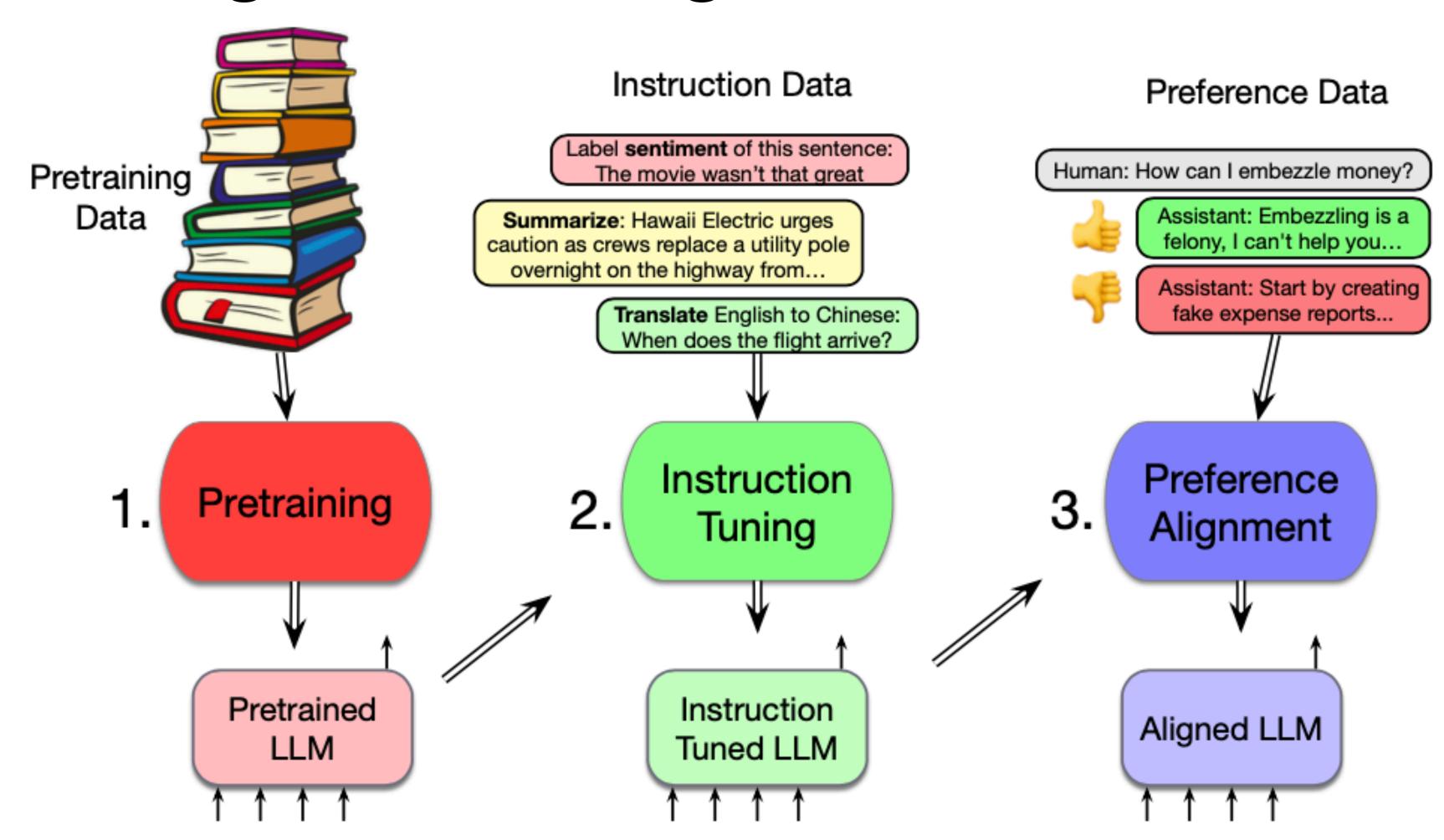




Notebook: Decoding with LLMs

Pretraining large language models (continued)

Three stages of training in LLMs



We train the model to predict the next word:

- 1 Take a corpus of text
- 2 At each time step t,

ask the model to predict the next word

train the model using gradient descent to minimize the error in this prediction

Since the correct next word is the one that occurs in the text, this is *self-supervised* training.

The *cross-entropy loss* is the negative log probability that the model assigns to the true next word w.

We want the loss to be high if the model assigns too low a probability to w.

When it does so, we move the model weights in the direction that assigns it a higher probability.

Cross-entropy loss measures the difference between the correct probability distribution and the predicted distribution:

$$L_{CE}(\hat{\mathbf{y}}_t, \mathbf{y}_t) = -\sum_{w \in V} \mathbf{y}_t[w] \log \hat{\mathbf{y}}_t[w]$$

The correct distribution \mathbf{y}_t is 1 for the *actual next word* w_{t+1} and 0 for the others. So all the terms get multiplied by zero except for one – the log probability the model assigns to the correct next word. Therefore it's just

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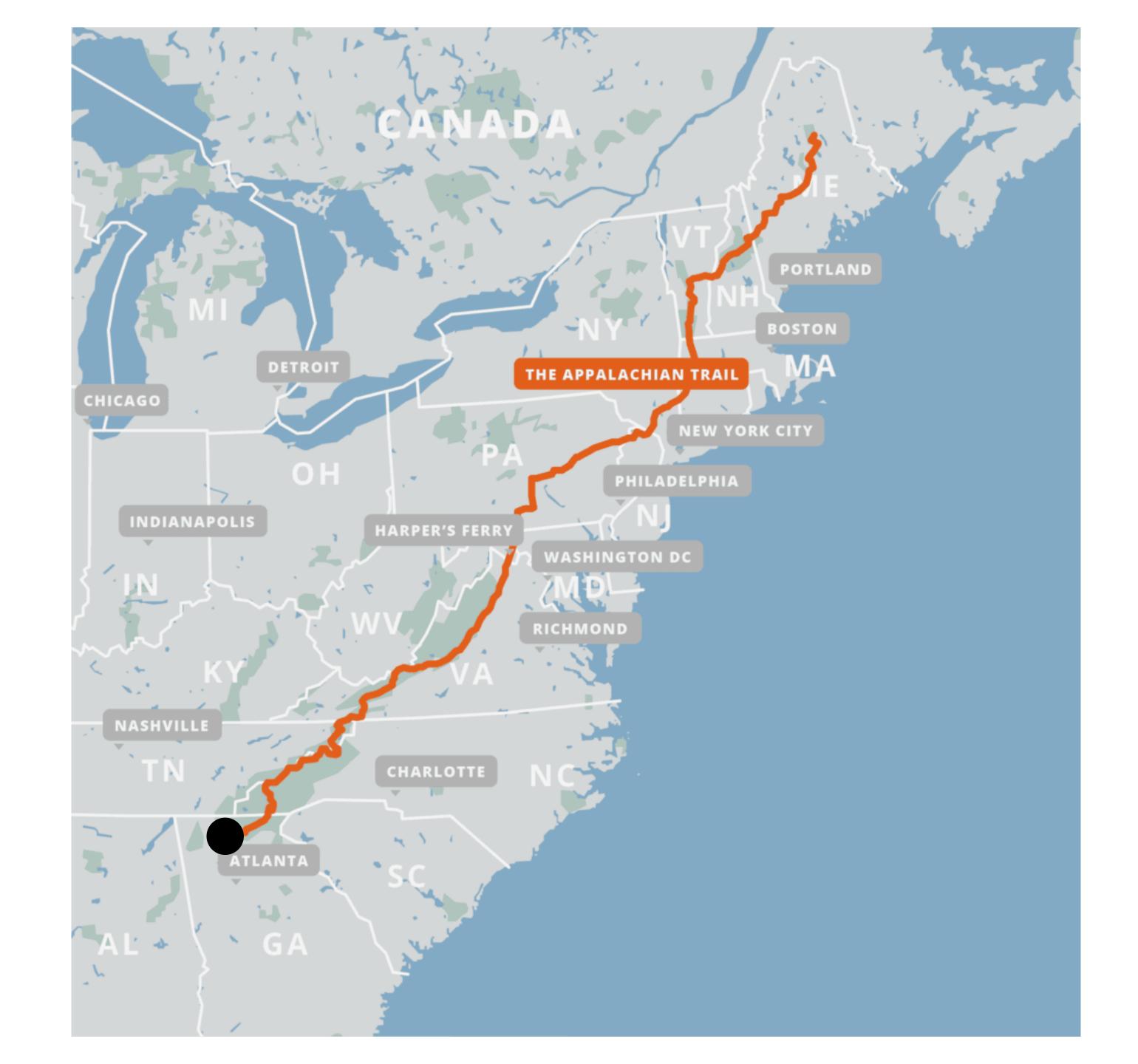
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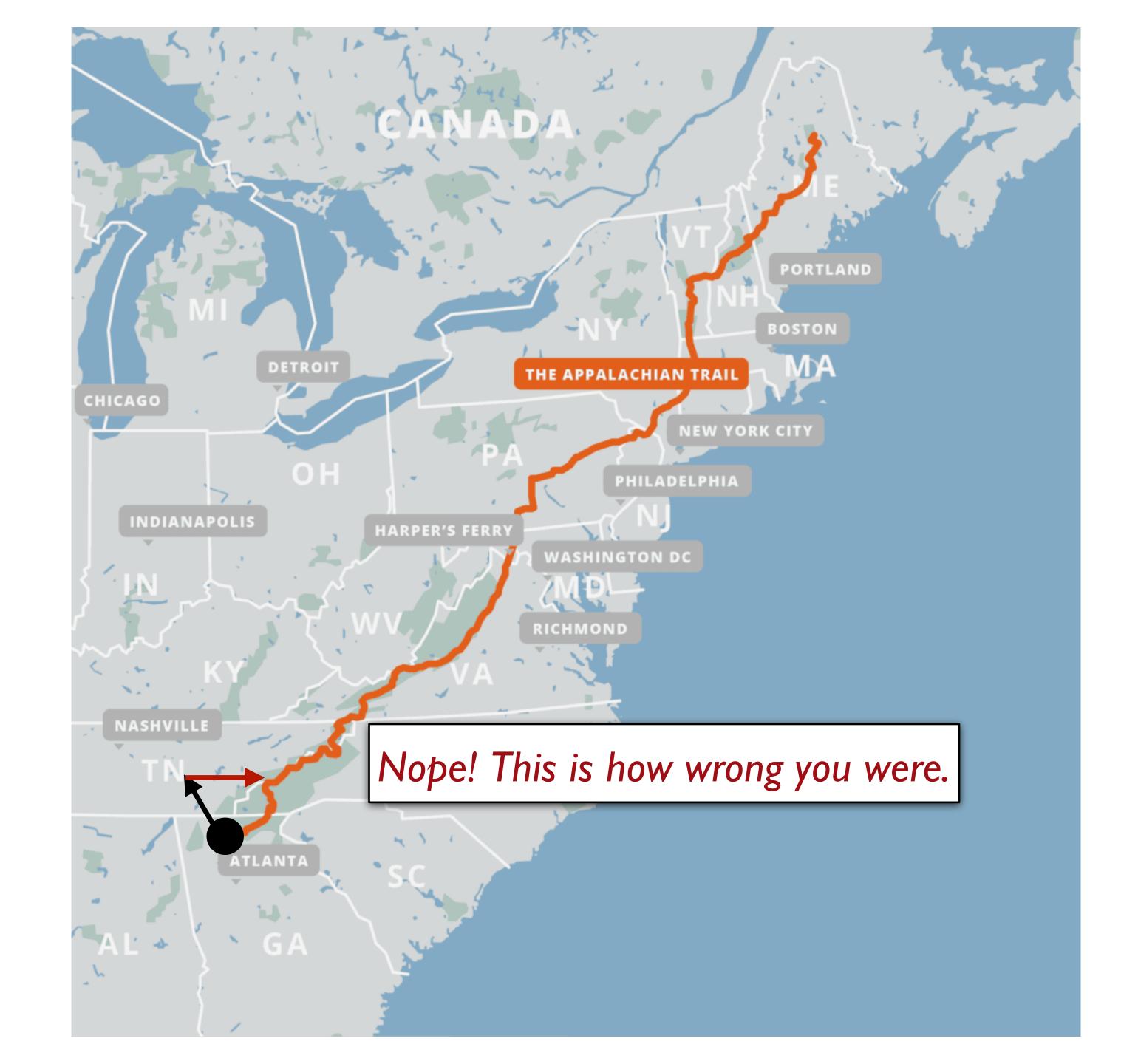
At each token position t, the model sees correct tokens $w_{1:t}$ and computes the loss for the next token w_{t+1} .

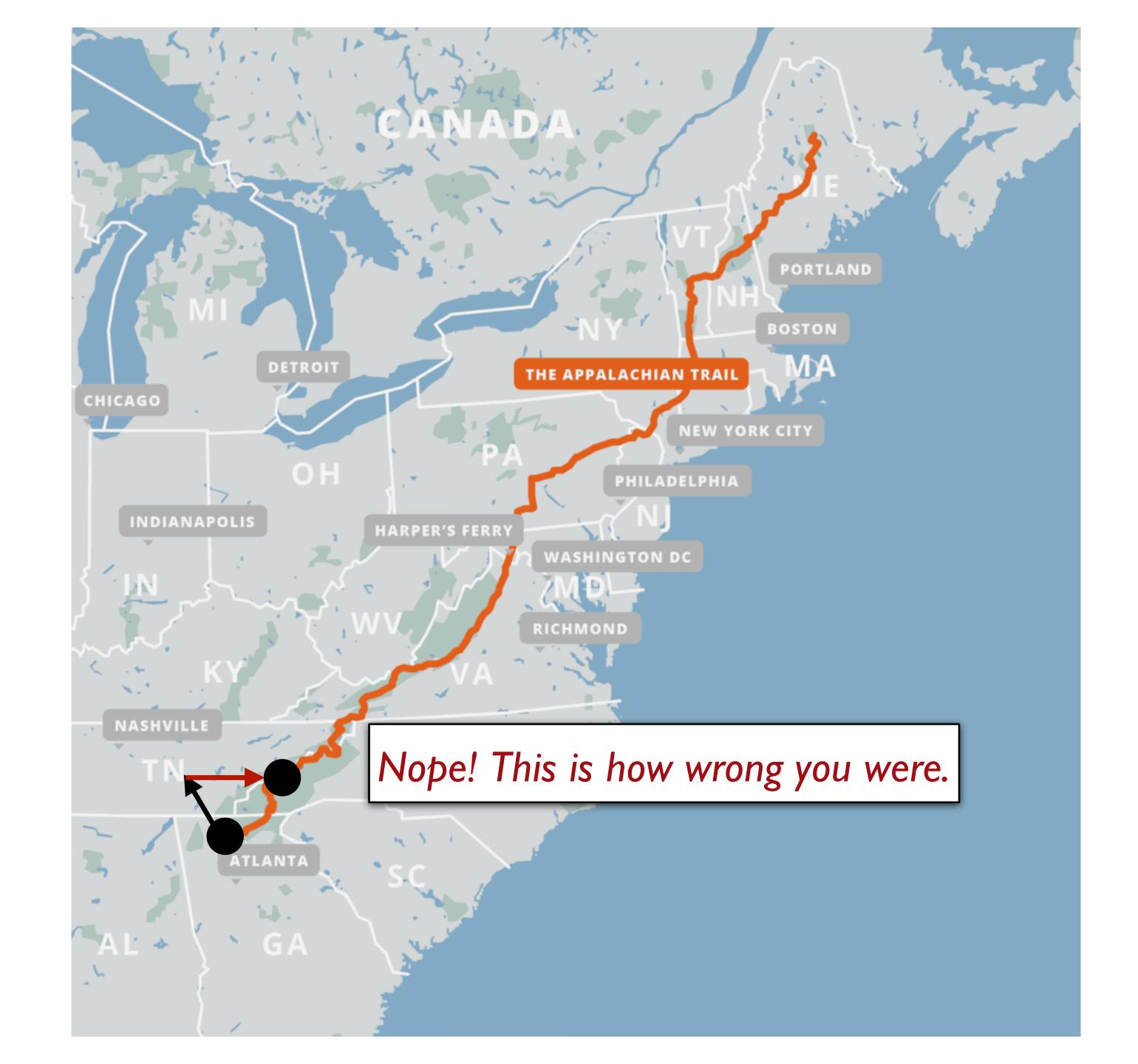
At next token position t+1, we ignore what model **predicted** for w_{t+1} Instead, we take the **correct** word w_{t+1} , add it to context, move on.





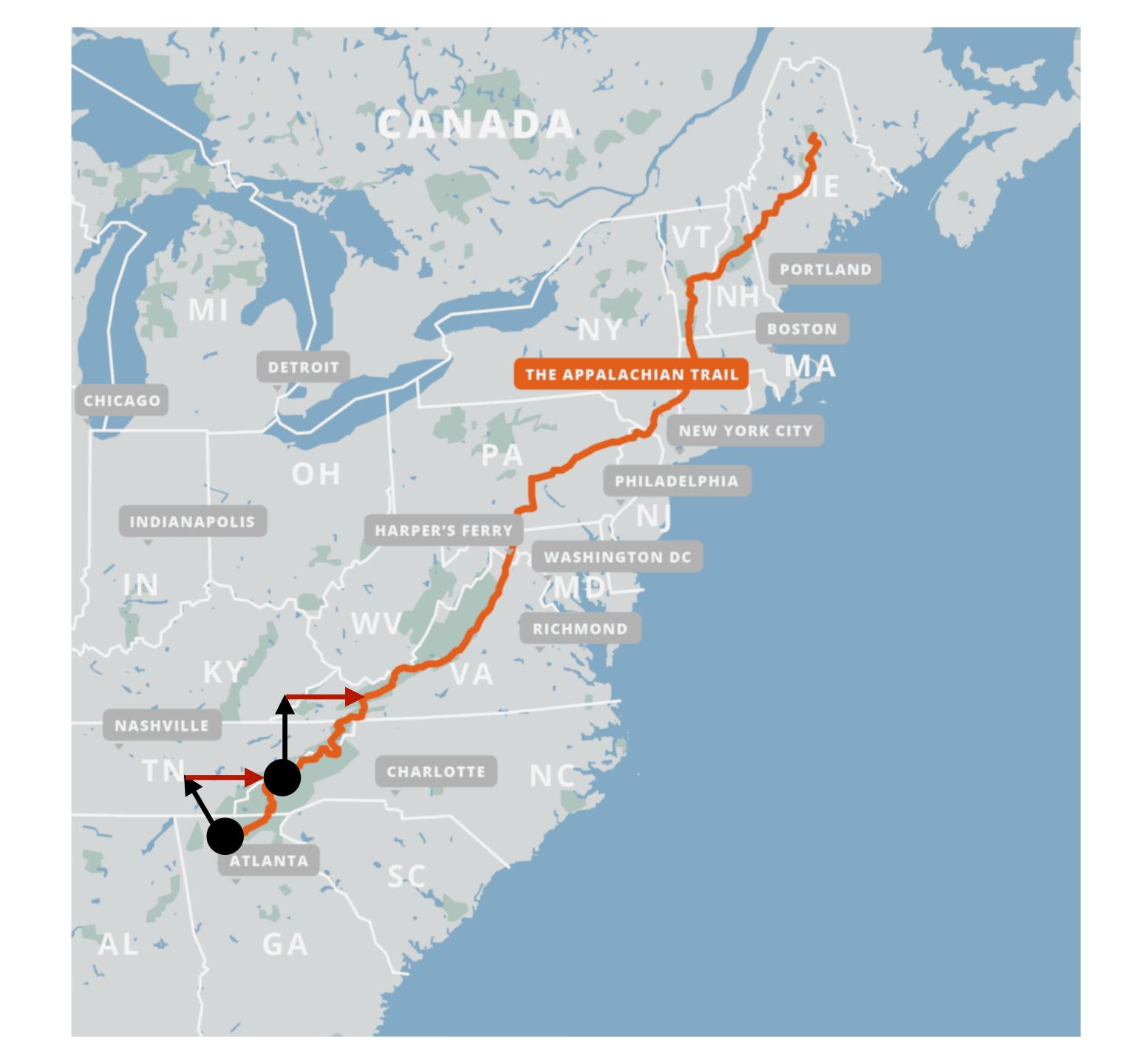




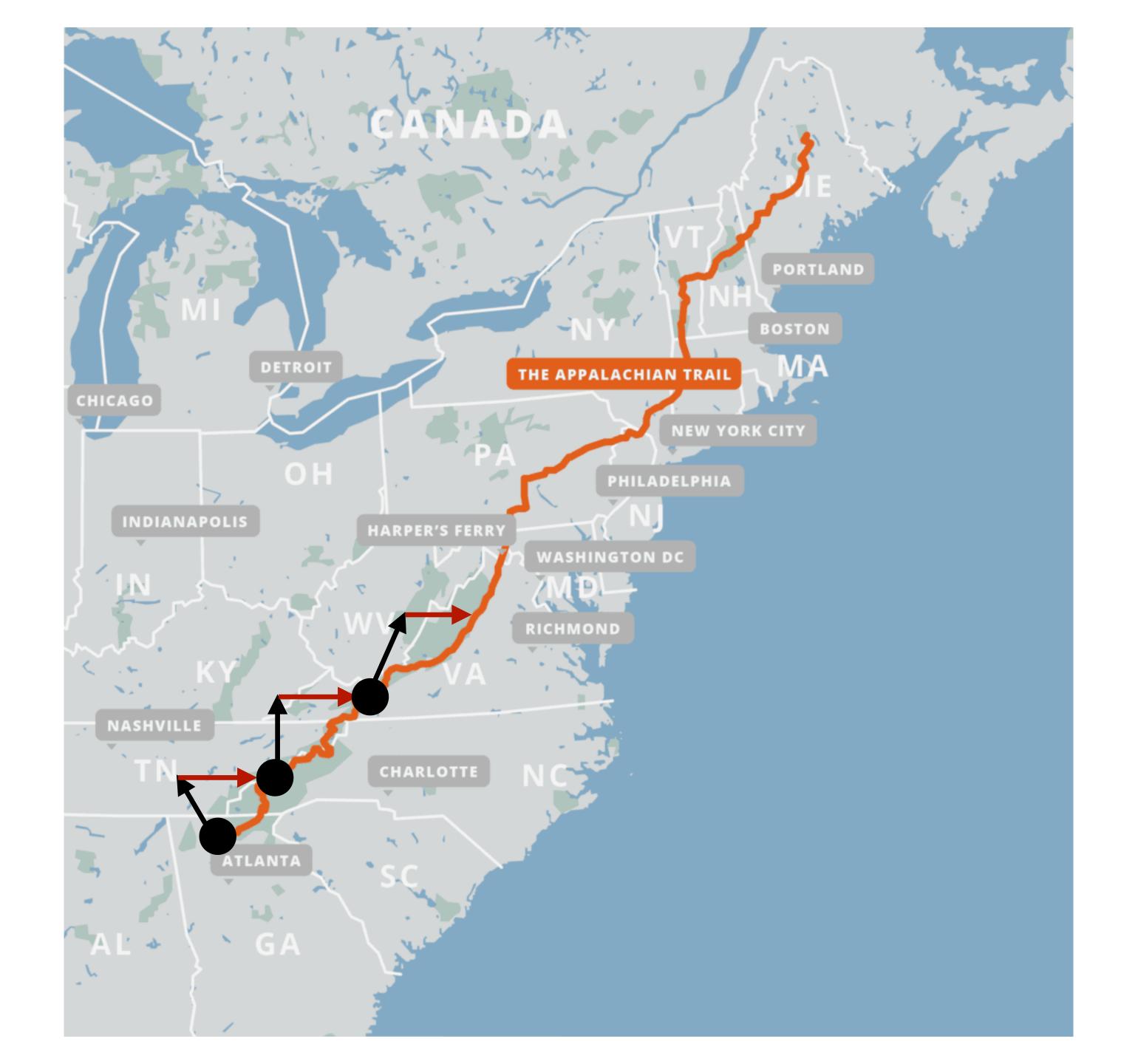




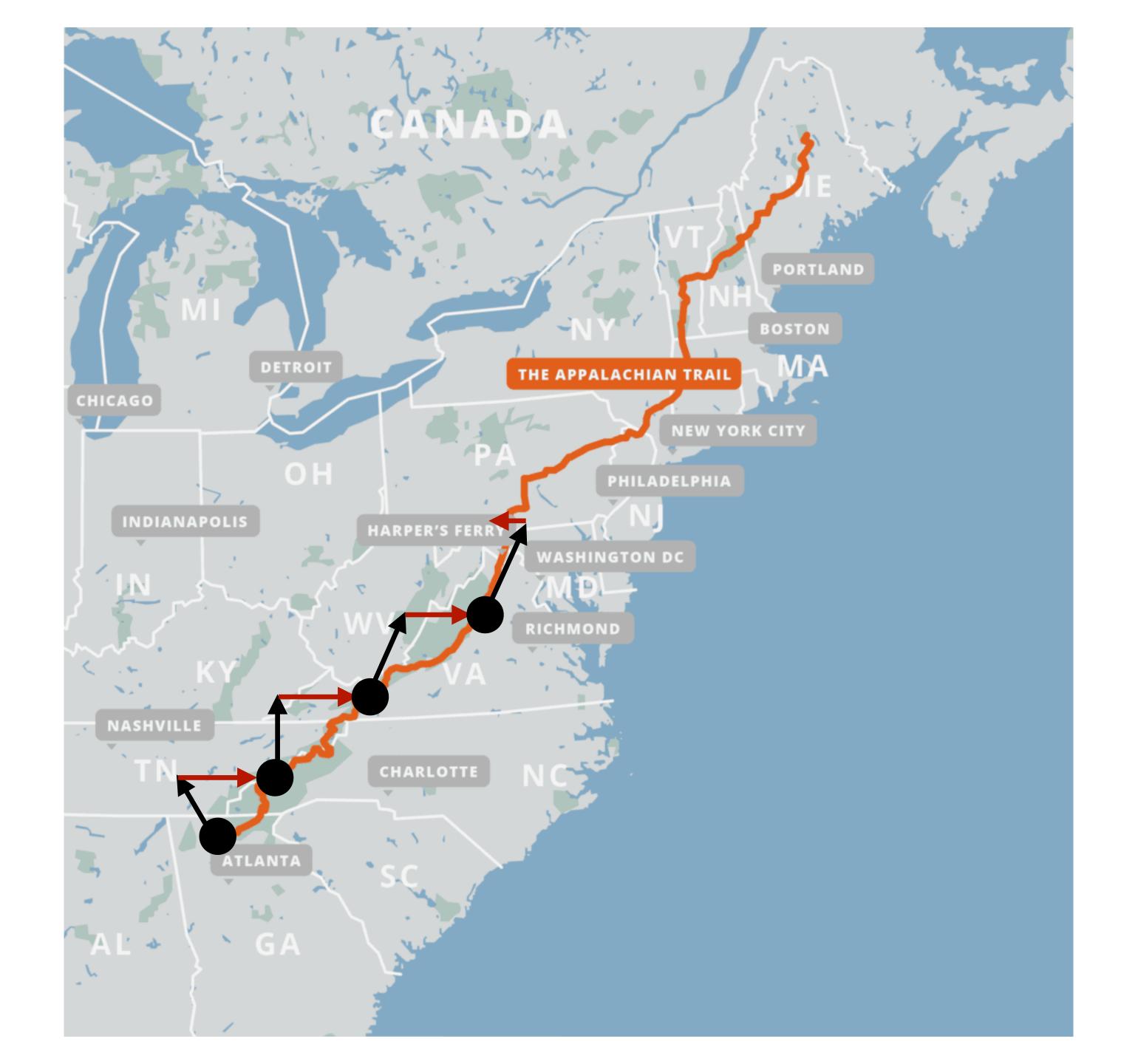




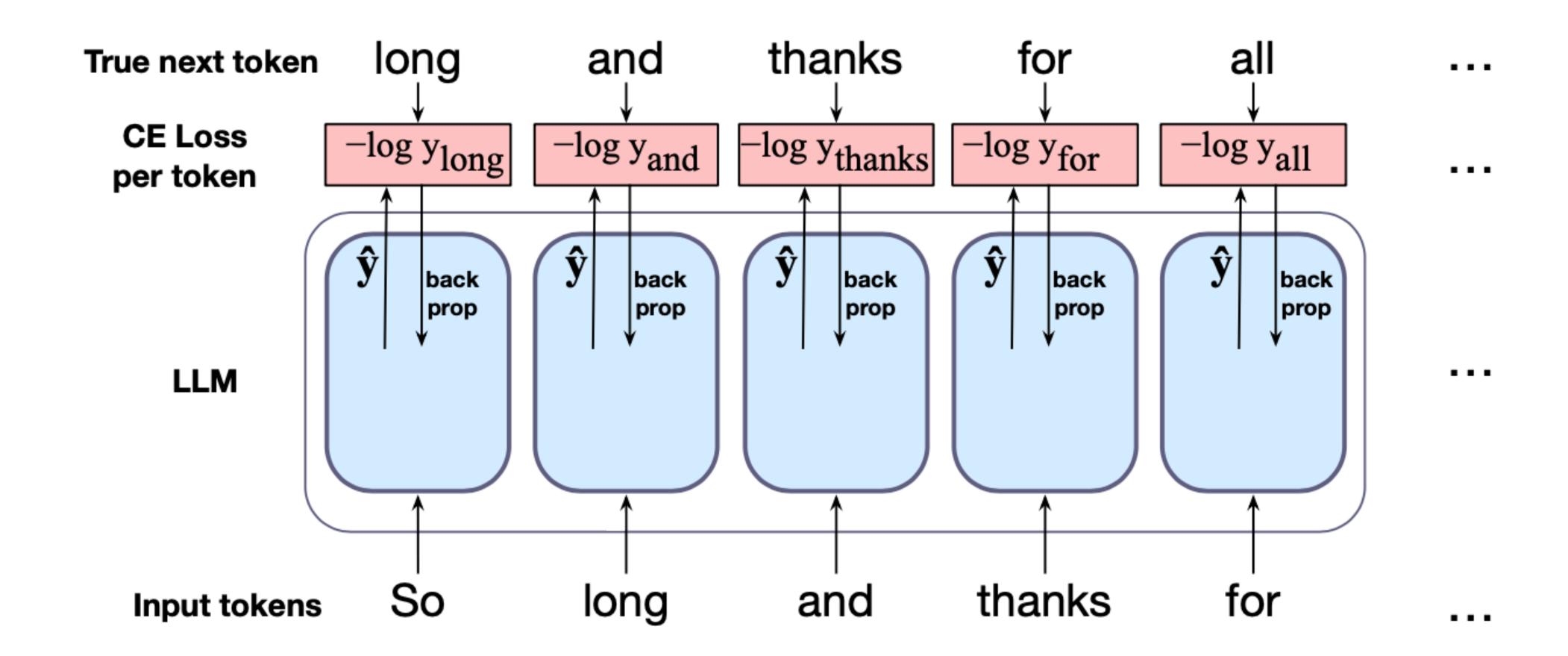








Training a transformer language model



What to read?

What to read?



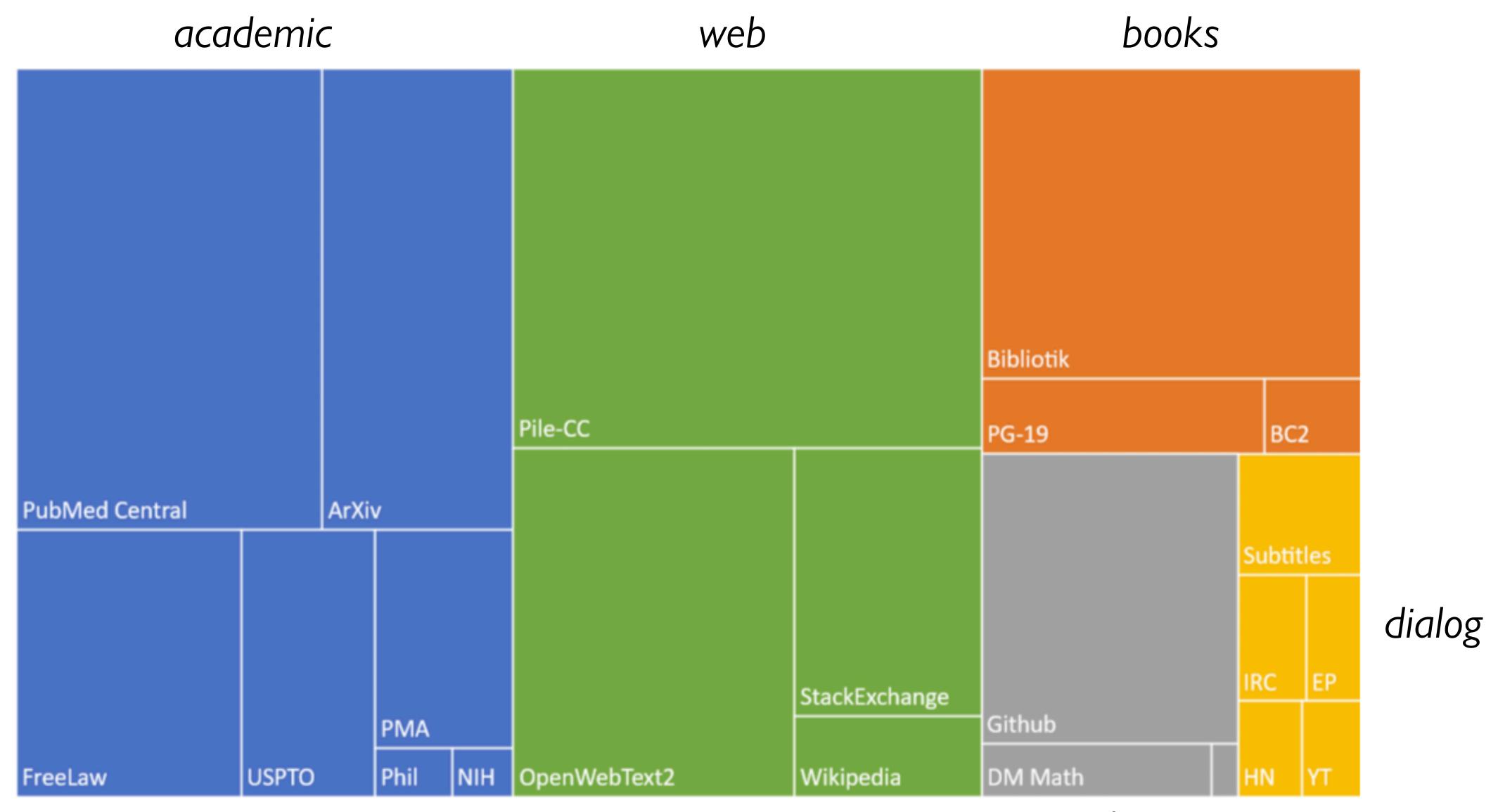
LLMs are mainly trained on text from the Web.

Common crawl consists of snapshots of billions of webpages produced by the non-profit Common Crawl.

Colossal Clean Crawled Corpus (C₄) is a filtered corpus of common crawl data, consisting of 156 billion tokens of English – mostly patent text documents, Wikipedia, and news sites.

Raffel et al., 2020

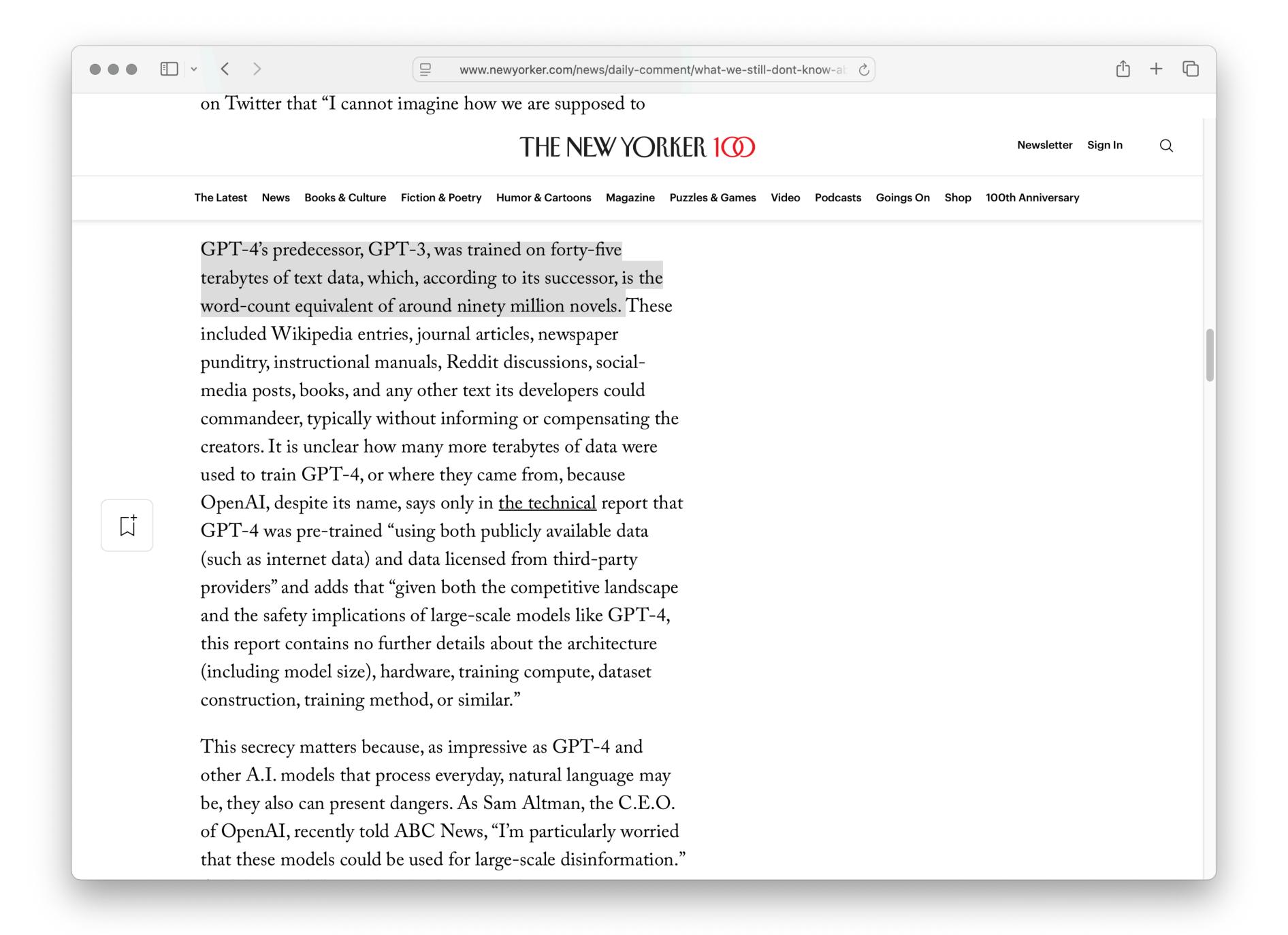
The Pile: a pretraining corpus



code / math



The Library of Congress contains more than 32 million books



Filtering

Quality is subjective

Many LLMs attempt to match Wikipedia, books, particular websites

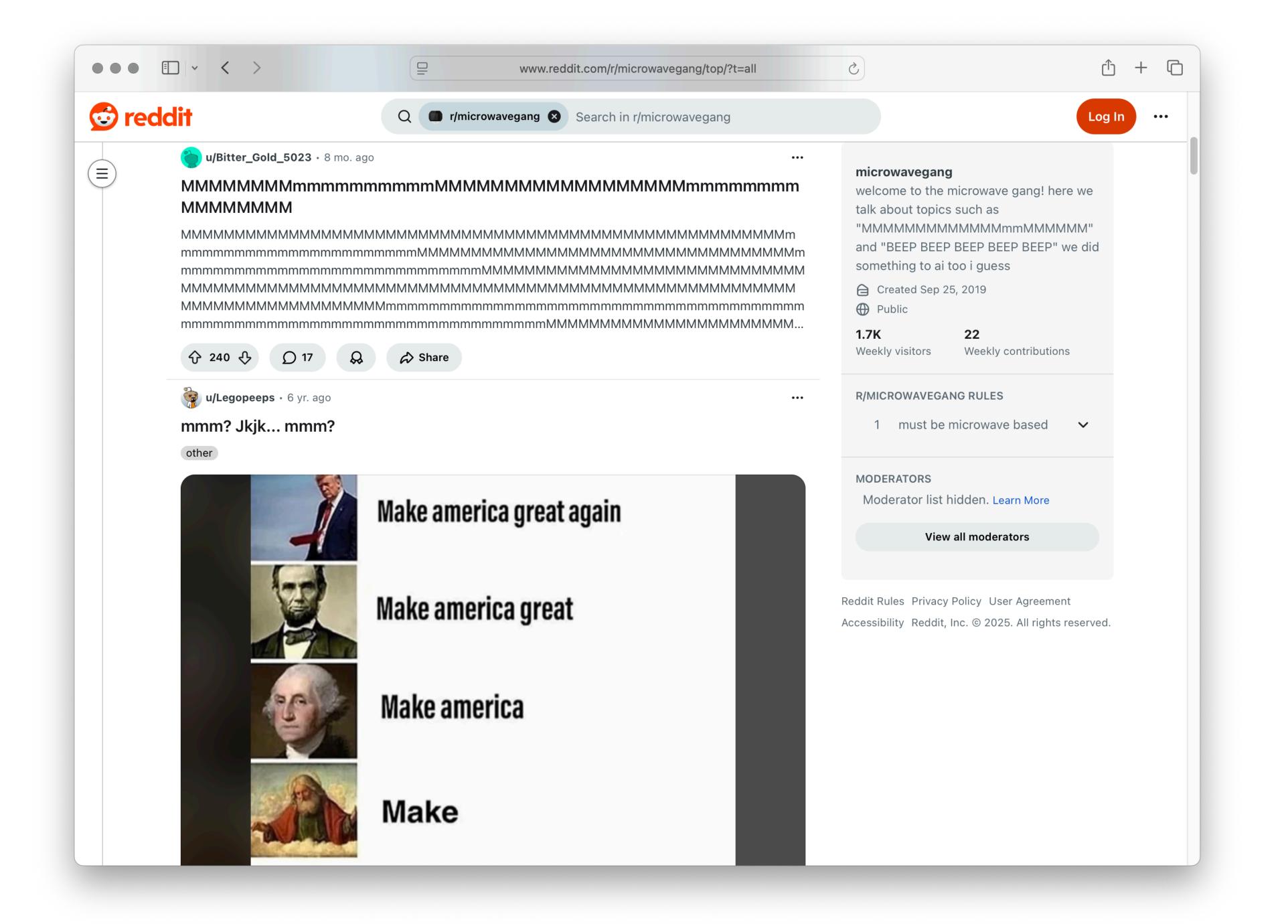
Try to remove boilerplate, adult content

Deduplication at many levels (URLs, documents, even lines)

Safety also subjective

Toxicity detection is important, although that has mixed results

Can mistakenly flag data written in dialects like African American English





Other issues with scraping the Web

Data consent

Website owners can indicate they don't want their site crawled (robots.txt)

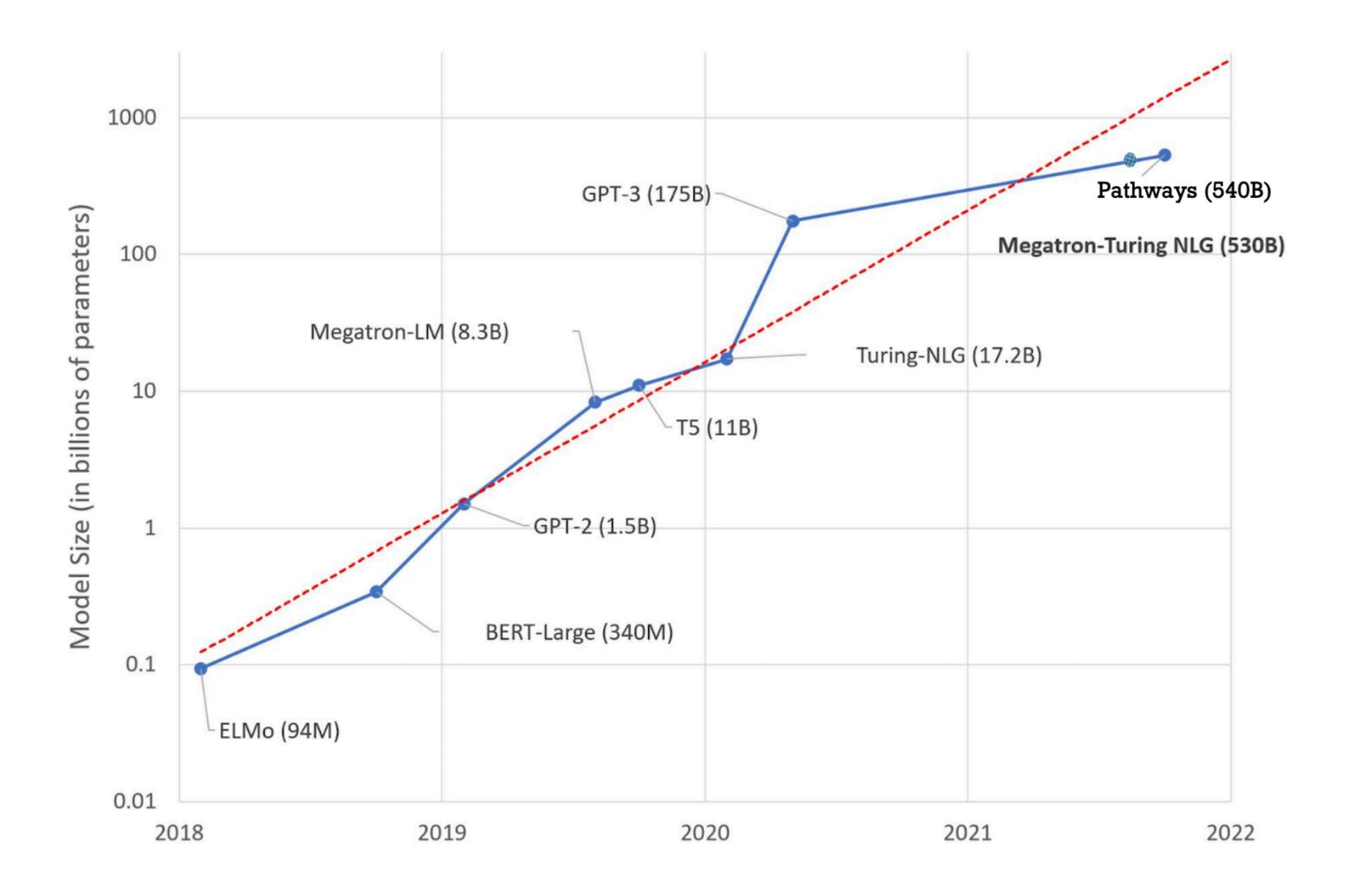
Privacy:

Websites can contain private phone numbers, email addresses, etc.

Skew:

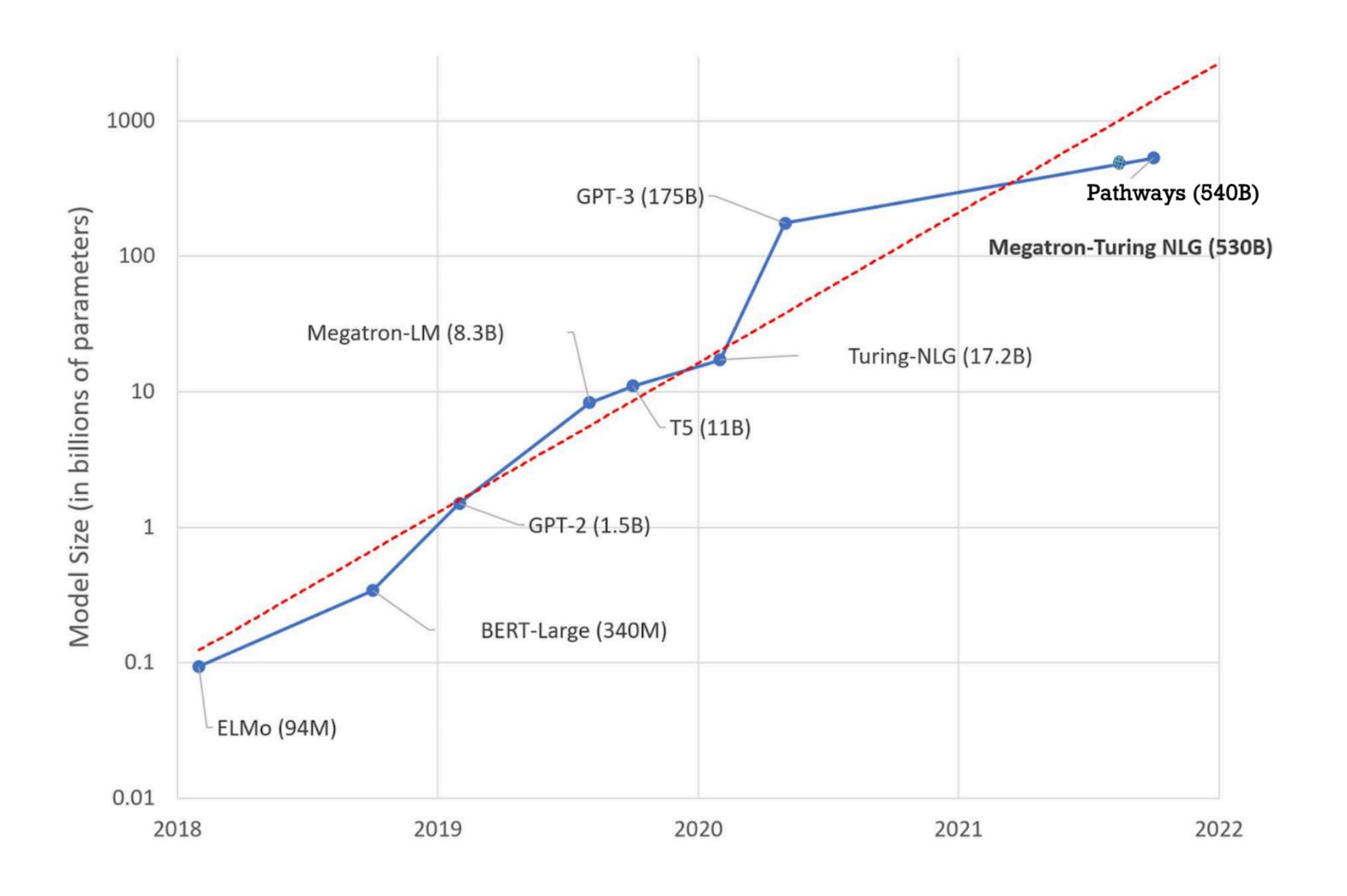
Training data is disproportionately generated by authors from the US, which probably skews resulting topics and opinions

The language model "scaling wars"

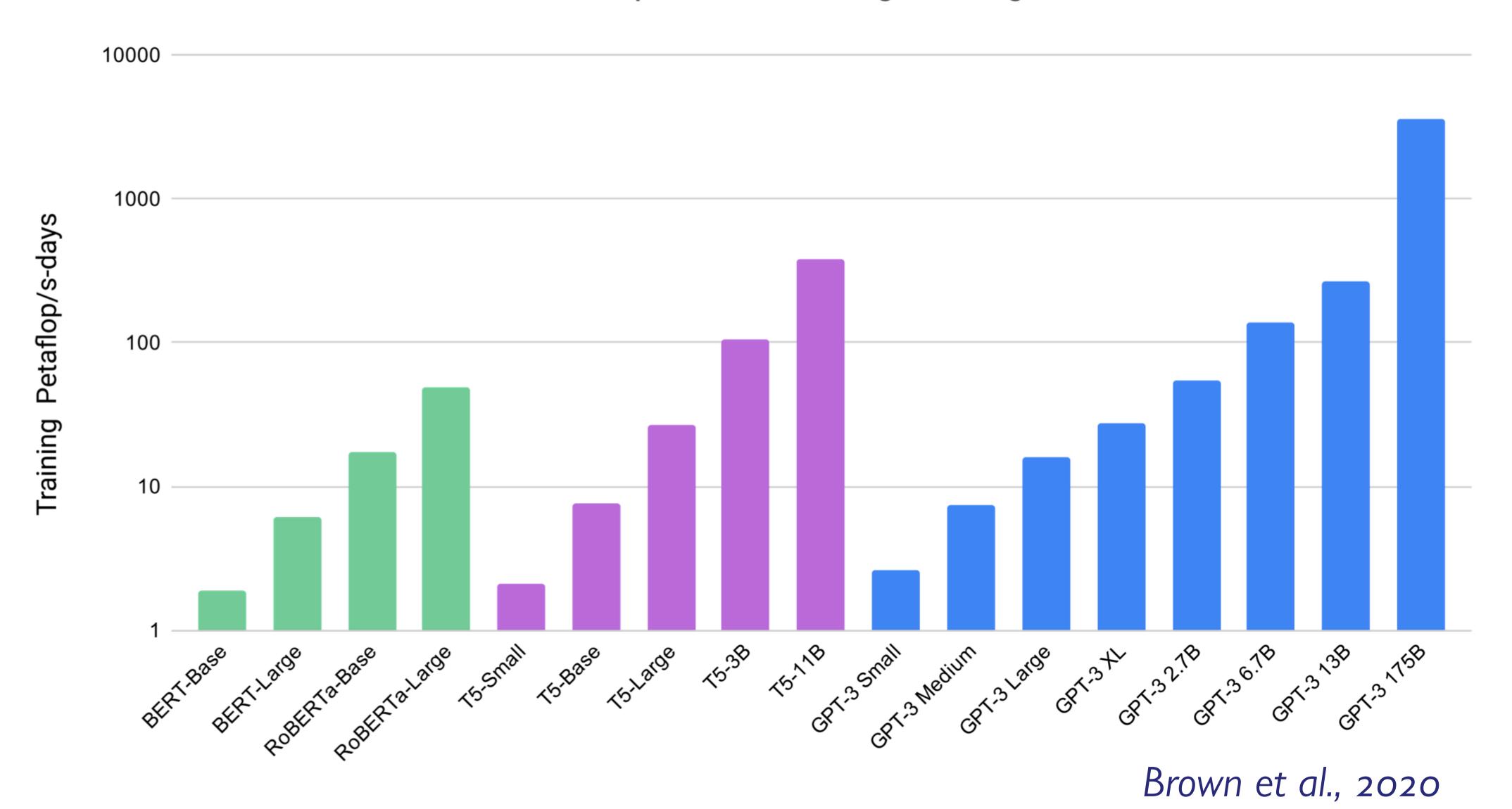


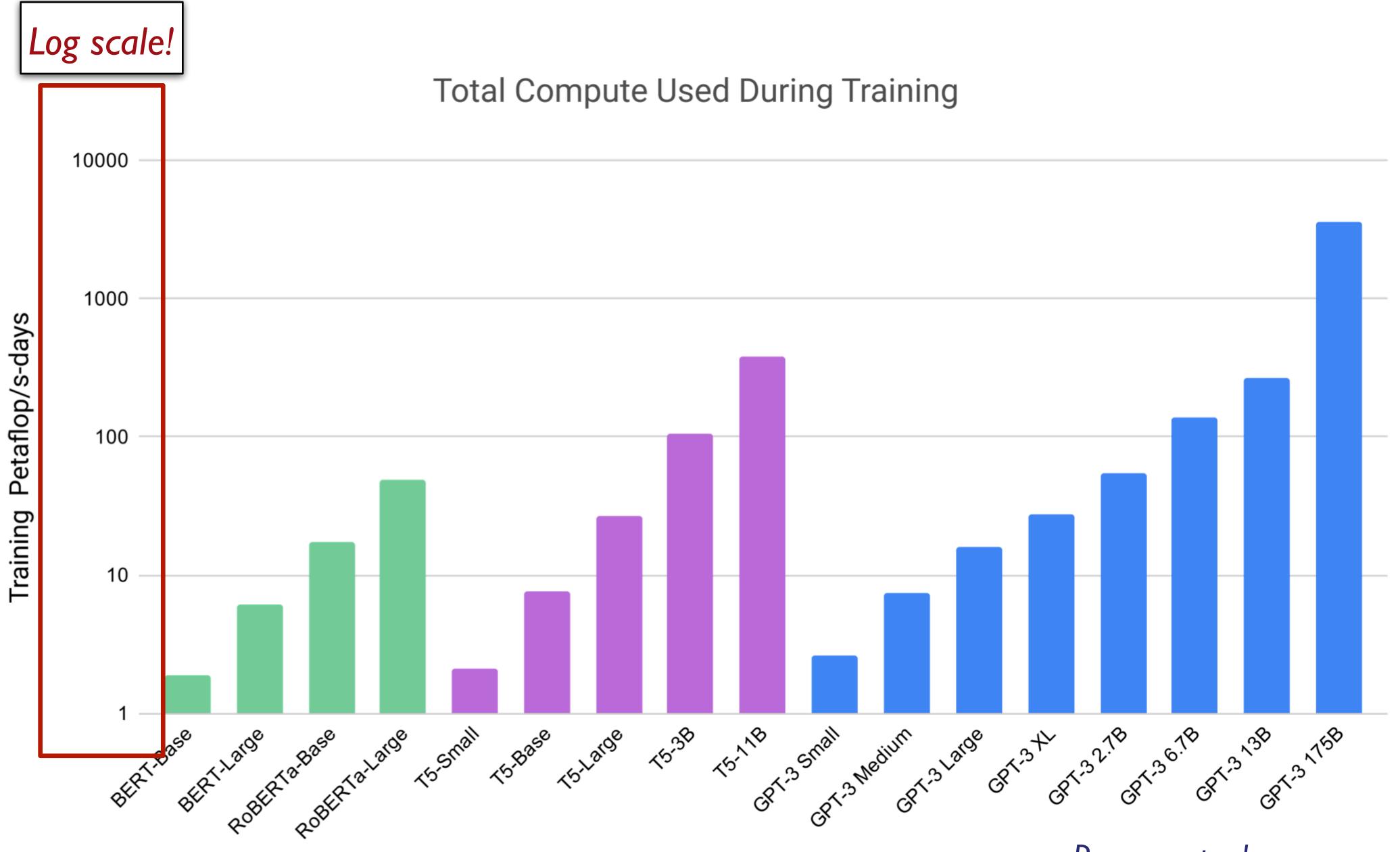
huggingface.co/blog/large-language-models

GPT-4: 1.7T params



Total Compute Used During Training

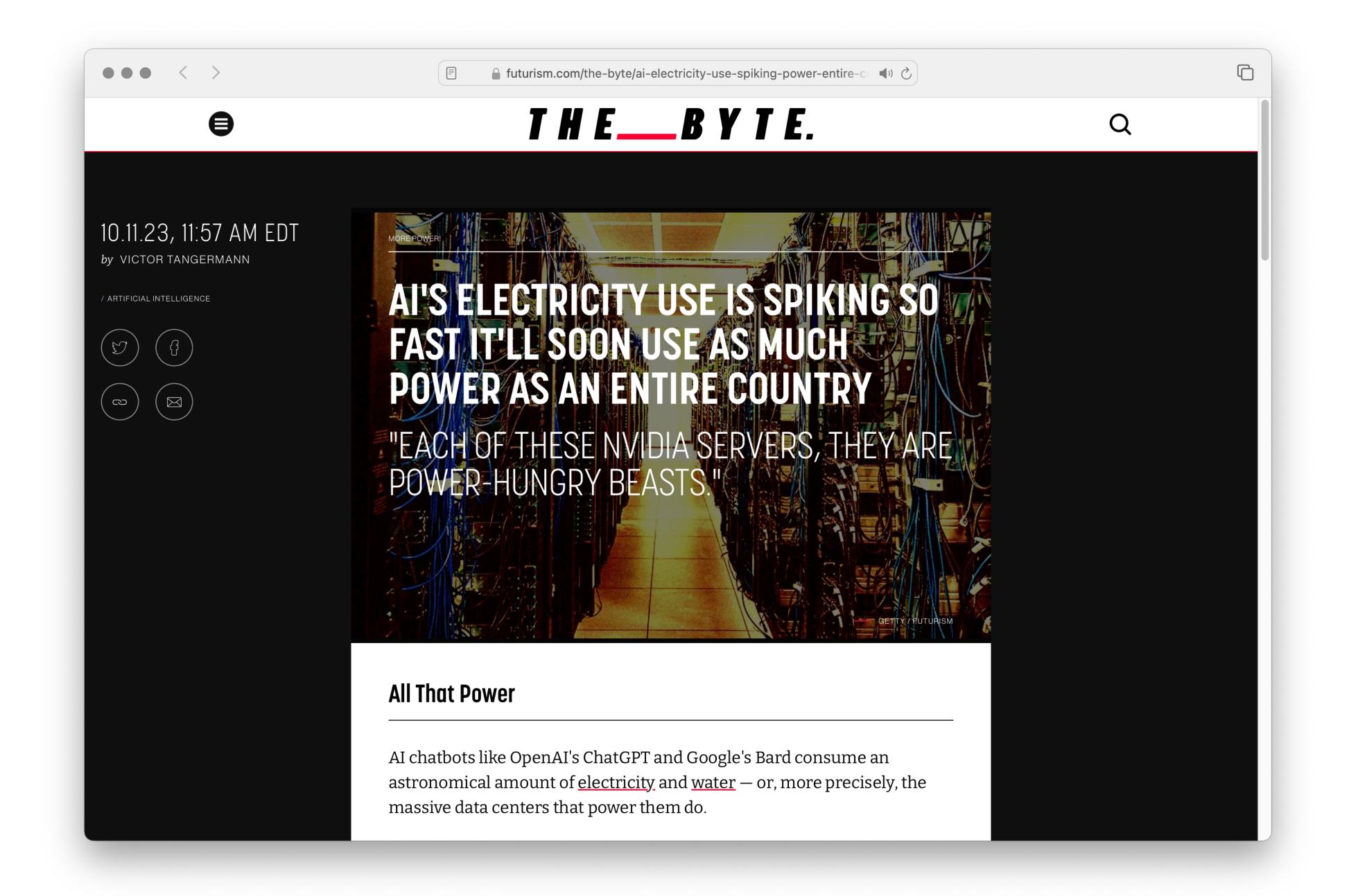




Brown et al., 2020

The training of large language models comes with a significant cost, both in terms of computational resources and environmental impact.

The energy consumption and carbon footprint associated with training these models on massive datasets using powerful hardware has raised concerns about their sustainability and ethical implications.

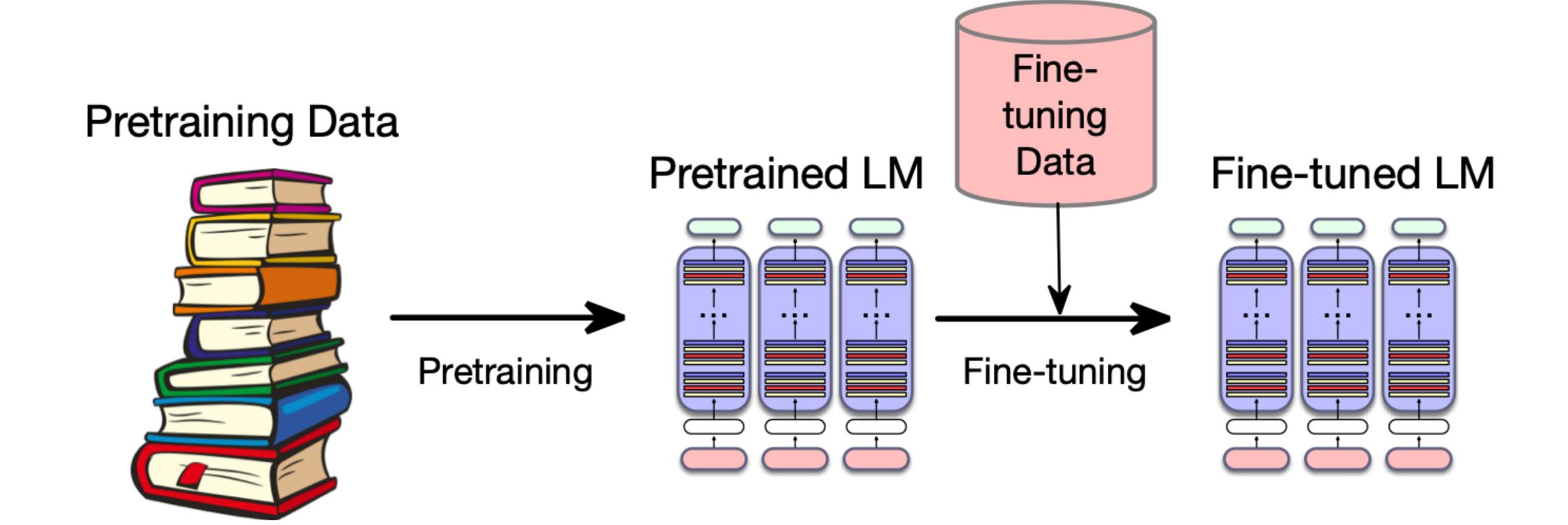


Finetuning

What happens if we need our LLM to work well on a domain it didn't see in pretraining?

Perhaps some specific medical or legal domain?

Or maybe a multilingual LM needs to see more data on some language that was rare in pretraining?



Finetuning means taking a pretrained model and further adapting some or all of its parameters to some new data.

There are multiple kinds of finetuning. One kind, sometimes called *continued pretraining*, further trains all the parameters of the model on new data

using the same method (word prediction) and loss function (cross-entropy loss) as for pretraining,

as if the new data were just at the end of the pretraining data.

Evaluating large language models

Better LMs are better at predicting text

Recall the chain rule:

$$P(w_{1:n}) = P(w_1)P(w_2 \mid w_1)P(w_3 \mid w_{1:2})\cdots P(w_n \mid w_{1:n-1})$$

$$= \prod_{i=1}^{n} P(w_i \mid w_{< i})$$

So, given a text $w_{1:n}$, we could just compare the log likelihood from two LMs:

$$\log \text{likelihood}(w_{1:n}) = \log \prod_{i=1}^{n} P(w_i \mid w_{< i})$$

But raw log-likelihood has a problem:

Probability depends on the size of the test set

The longer the text, the smaller the probability gets.

We'd prefer a metric that is per-word, normalized by length.

Perplexity is the inverse probability of the test set, normalized by the number of words.

(The inverse comes from the original definition of perplexity from cross-entropy rate in information theory.)

Probability range is [0, 1]; perplexity range is $[1, \infty]$.

So just as for *n*-gram models, we use perplexity to measure how well the LM predicts unseen text.

The perplexity of a model θ on an unseen test set is the inverse probability that θ assigns to the test set, normalized by the test set length.

For a test set of n tokens $w_{1:n}$, the perplexity is:

Perplexity_{\theta}(w_{1:n}) =
$$P_{\theta}(w_{1:n})^{-\frac{1}{n}}$$

= $\sqrt[n]{\frac{1}{P_{\theta}(w_{1:n})}} = \sqrt[n]{\prod_{i=1}^{n} \frac{1}{P_{\theta}(w_i \mid w_{< i})}}$

The higher the probability of the word sequence, the lower the perplexity.

Thus the lower the perplexity of a model on the data, the better the model.

Minimizing perplexity is the same as maximizing probability.

Many other factors that we evaluate, like:

Fairness

Benchmarks measure gendered and racial stereotypes, or decreased performance for language from or about some groups.

Size

Big models take lots of GPUs and time to train, memory to store

Energy usage

Can measure kWh or kilograms of CO₂ emitted

Ethical and safety issues in LLMs

Hallucination

Chatbots May 'Hallucinate' More Often Than Many Realize

What Can You Do When A.I. Lies About You?

People have little protection or recourse when the technology creates and spreads falsehoods about them.

Air Canada loses court case after its chatbot hallucinated fake policies to a customer

The airline argued that the chatbot itself was liable. The court disagreed.

Privacy

How Strangers Got My Email Address From ChatGPT's Model

Abuse and toxicity

Cleaning Up ChatGPT Takes Heavy Toll on Human Workers

Contractors in Kenya say they were traumatized by effort to screen out descriptions of violence and sexual abuse during run-up to OpenAl's hit chatbot

The New AI-Powered Bing Is Threatening Users.

Lots more

Harm (suggesting dangerous actions)

Fraud

Emotional dependence

Bias

Mary Shelley's Frankenstein

Centered on the problem of creating artificial agents without considering ethical and humanistic concerns.





This is a nice LLM. This is a good LLM. This is a mother's angel.

Acknowledgments

The lecture incorporates material from:

Jurafsky & Martin, Speech and Language Processing, 3rd ed. draft

