



# Session-Typed Concurrent Contracts

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HANNAH GOMMERSTADT

LIMIN JIA & FRANK PFENNING

# Sorting Process

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# Sorting Process

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← 3



# Sorting Process



← 3

← 5



# Sorting Process

SORTING  
SORTING



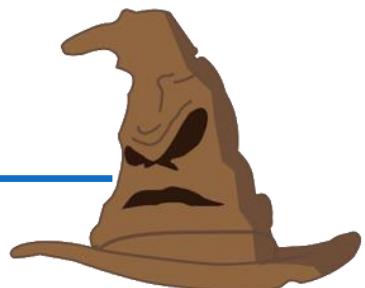
← 3



← 5



← 4



# Sorting Process

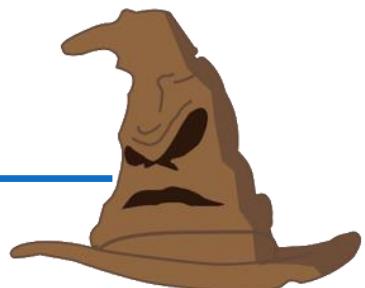
SORTING  
SORTING



← 3



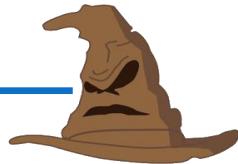
← 5



← 4

# Session Types?!

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$list = \oplus \{cons: int \wedge list; nil: 1\}$

# Session Types?!

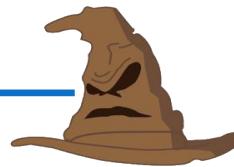
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$list = \oplus \{cons: int \wedge list; nil: 1\}$

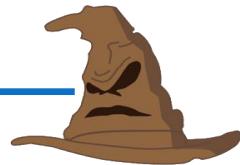


$\leftarrow cons$

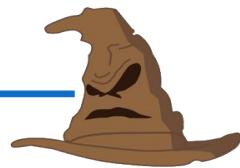


# Session Types?!

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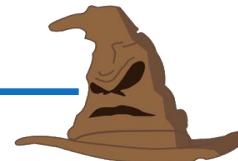

$$list = \oplus \{cons: int \wedge list; nil: 1\}$$


← cons

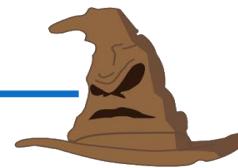

$$int \wedge list;$$

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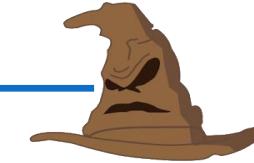
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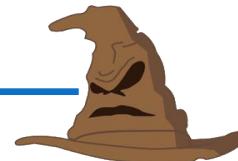

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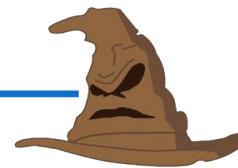


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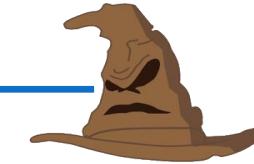
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$$list = \oplus \{cons: int \wedge list; nil: 1\}$$


← cons


$$int \wedge list;$$


← 5


$$list;$$

# Session Types as Contracts

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- Session types prescribe communication contracts between processes
- Dynamically typechecked because processes are untrusted
- Prior work (POPL 2016) on monitoring and blame assignment

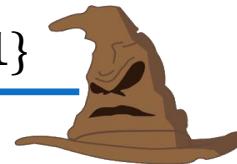
# Sorting Contract

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Contract we have:



$$list = \oplus \{cons: int \wedge list; nil: 1\}$$



Contract we want:

All received integers are  
in ascending order

# Challenge

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How do we dynamically monitor contracts that cannot be expressed as session type?

# Contributions

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- Partial-identity processes that monitor stateful contracts dynamically
- Monitor generation from type refinements
- Method for verifying that monitors are partial identities

# Partial Identity Monitors!

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- Processes written in the same language as all other code
- Abort if contract is violated, otherwise are transparent
- Check properties by using internal state



# Sorting Monitor

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SORTING  
SORTING

# Sorting Monitor

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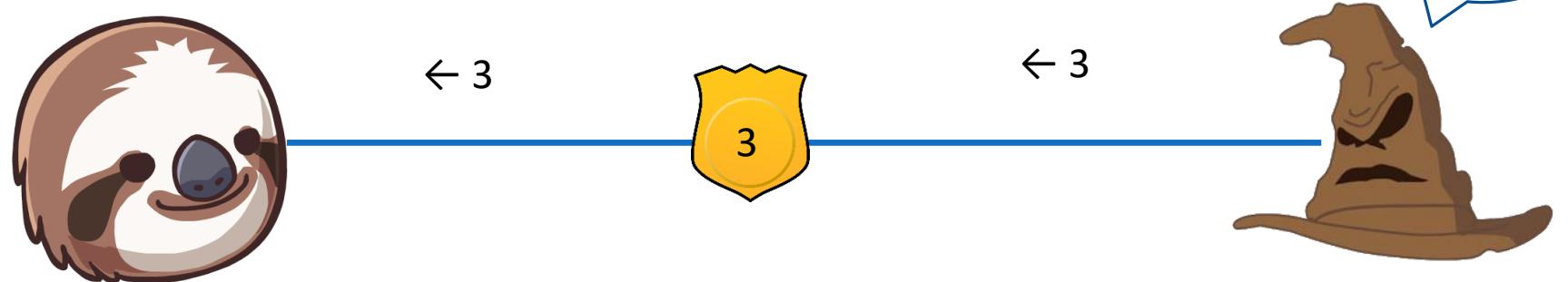


← 3

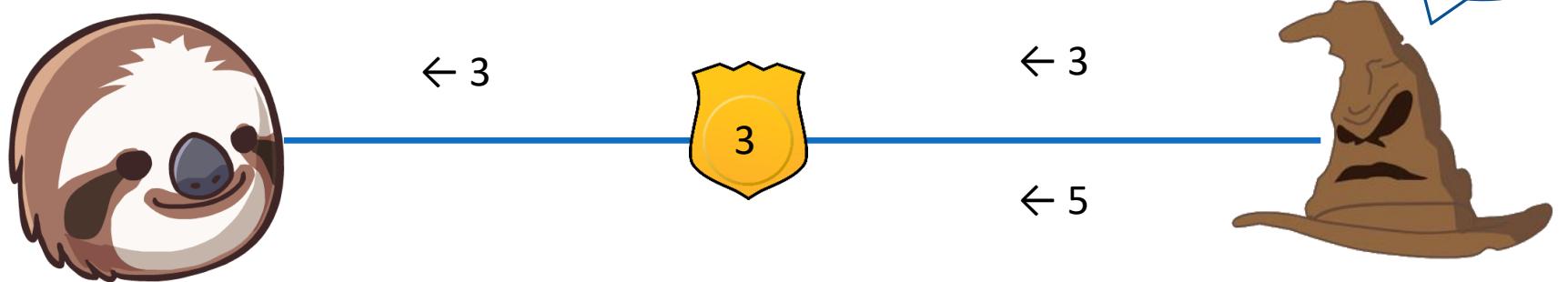


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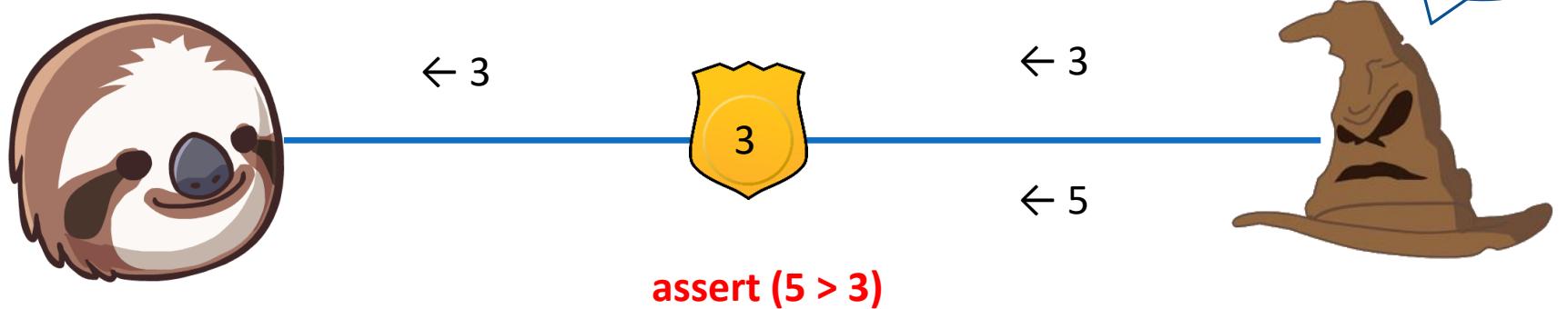
# Sorting Monitor



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← 3



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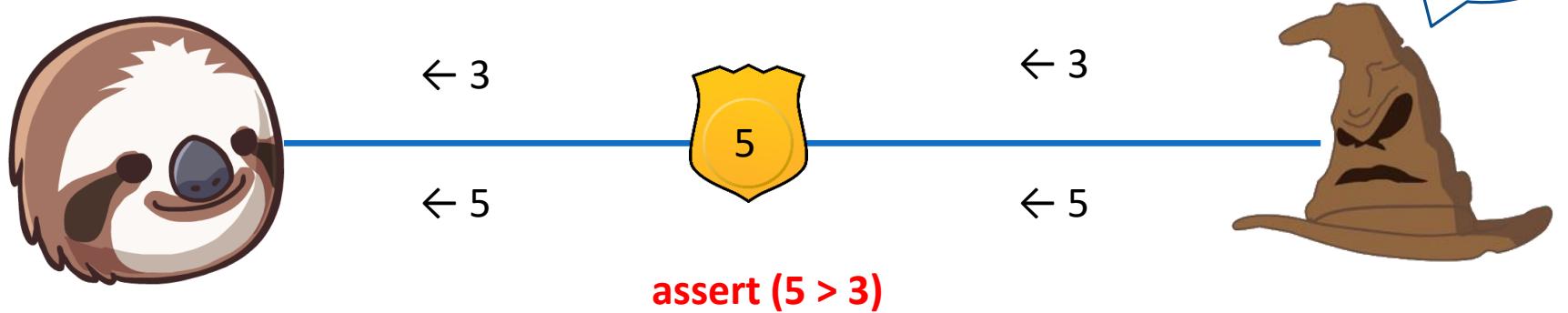


← 5

**assert (5 > 3)**



# Sorting Monitor



# Sorting Monitor



← 3

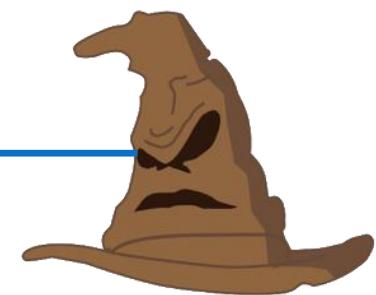


← 5

← 3



**assert (5 > 3)**



SORTING  
SORTING

# Sorting Monitor



← 3



← 5

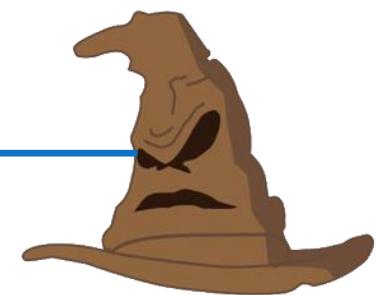
← 3



**assert (5 > 3)**



← 4



SORTING  
SORTING

# Sorting Monitor



← 3



← 5

← 3

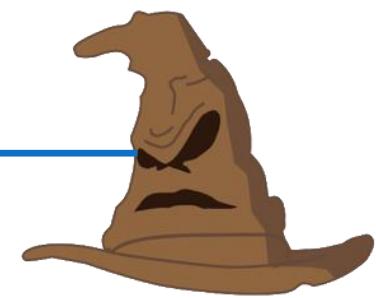


**assert (5 > 3)**



← 4

**assert (4 > 5)**



# Sorting Monitor



← 3



← 5

**assert (5 > 3)**

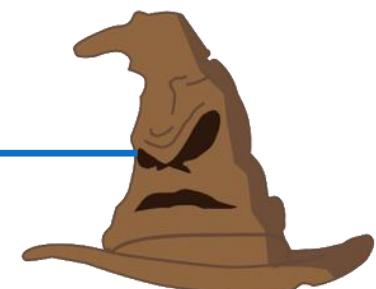
← 3



← 5



← 4



**assert (4 > 5)**

SORTING  
SORTING

# List Identity Process

list\_id : list  $\leftarrow$  list

a  $\leftarrow$  list\_id b =

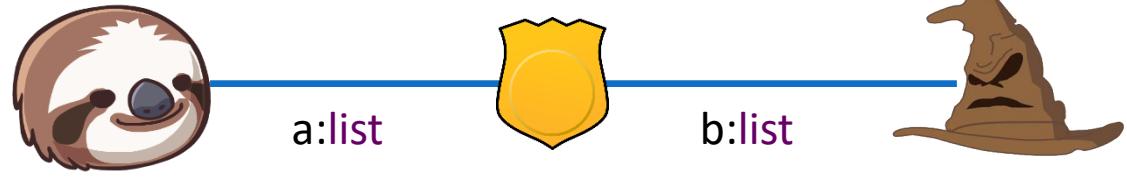
case b of

| nil  $\Rightarrow$  a.nil; wait b; close a

| cons  $\Rightarrow$  x  $\leftarrow$  recv b;

a.cons(x);

a  $\leftarrow$  list\_id b;



$$list = \oplus \{cons:int \wedge list; nil:1\}$$

# List Identity Process

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a  $\leftarrow$  list\_id b =

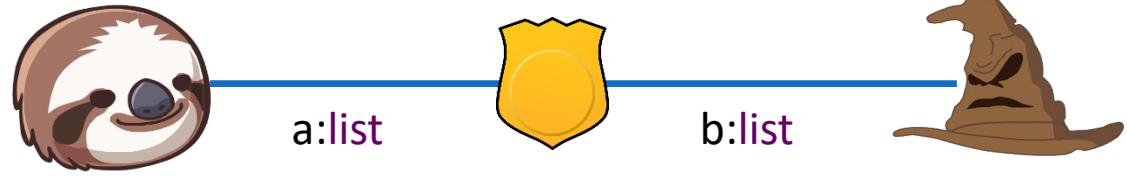
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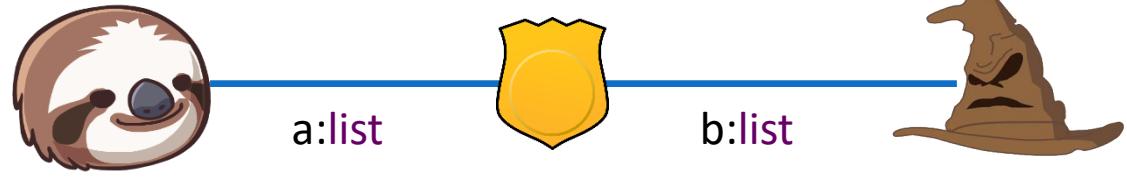
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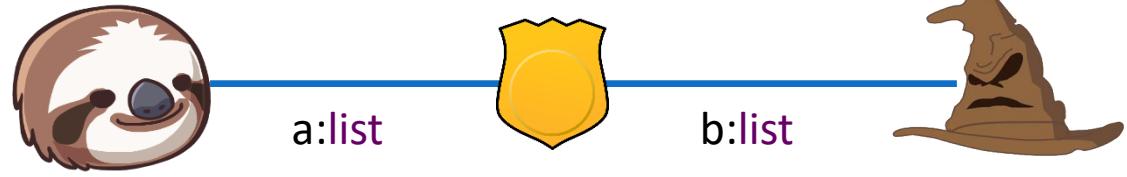
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# List Identity Process

list\_id : list  $\leftarrow$  list

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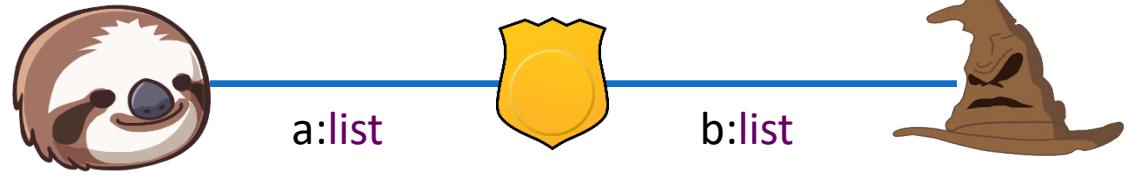
case b of

| nil  $\Rightarrow$  a.nil; wait b; close a

| cons  $\Rightarrow$  x  $\leftarrow$  recv b;

a.cons(x);

a  $\leftarrow$  list\_id b;



# Sorted List

```
asc_mon: list ← int option, list ::;
```

```
a ← asc_mon bound b =
```

```
case b of
```

```
| nil ⇒ a.nil; wait b; close a
```

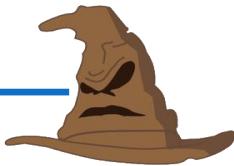
```
| cons ⇒ x ← recv b;
```



a:list



b:list



*list* =  $\oplus \{cons: int \wedge list; nil: 1\}$

```
case bound of
```

```
| None ⇒ a.cons(x); a ← asc_mon (Some x) b
```

```
| Some y ⇒ assert (x >= y);
```

```
a.cons(x); a ← asc_mon (Some x) b;
```

# Other Exciting Contracts

Contract	Monitor State
List of parentheses is well matched	Stack – push for (, pop for )
List of integers corresponds to correctly serialized binary tree	Stack – push for node, pop for leaf
Sorting procedure permutes elements of a list	Sum of hash values of each element
Doubling process mapped over a list of integers is monotonic	Input integer
Refinements on integers	None
Factoring procedures outputs integers that multiply to input	Input integer

# Checking Refinements

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- Encode refinements as type casts
- Can generate a partial identity monitor to check the refinement

$$\{A\}_a \Leftarrow \{B\}_b$$

# Integer Refinement Translation

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$$\{n: \textcolor{blue}{int} \mid \textcolor{green}{n > 0} \wedge \textcolor{violet}{A}\}_a \Leftarrow \{n: \textcolor{blue}{int} \wedge \textcolor{violet}{B}\}_b$$

# Integer Refinement Translation

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$$\{n: \textcolor{blue}{int} \mid \textcolor{green}{n > 0} \wedge \textcolor{violet}{A}\}_a \Leftarrow \{n: \textcolor{blue}{int} \wedge \textcolor{violet}{B}\}_b$$

```
x ← recv b;  
send a x;
```

# Integer Refinement Translation

---

$$\{n: \textit{int} \mid n > 0 \wedge A\}_a \Leftarrow \{n: \textit{int} \wedge B\}_b$$

```
x ← recv b;  
assert (x > 0)  
send a x;
```

# Integer Refinement Translation

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$$\{n: \textcolor{blue}{int} \mid n > 0 \wedge \textcolor{violet}{A}\}_a \Leftarrow \{n: \textcolor{blue}{int} \wedge \textcolor{violet}{B}\}_b$$

```
x ← recv b;  
assert (x > 0)  
send a x;  
 $\{\textcolor{violet}{A}\}_a \Leftarrow \{\textcolor{violet}{B}\}_b$ 
```

# Label Refinement Translation

---

$$\oplus \{\text{cons}: \text{int} \wedge \text{list}\}_a \Leftarrow \oplus \{\text{cons}: \text{int} \wedge \text{list}; \text{nil}: 1\}_b$$

# Label Refinement Translation

---

$$\oplus \{\text{cons}: \text{int} \wedge \text{list}\}_a \Leftarrow \oplus \{\text{cons}: \text{int} \wedge \text{list}; \text{nil}: 1\}_b$$

case b of

| nil =>

| cons =>

# Label Refinement Translation

---

$$\oplus \{\text{cons}: \text{int} \wedge \text{list}\}_a \Leftarrow \oplus \{\text{cons}: \text{int} \wedge \text{list}; \text{nil}: 1\}_b$$

case b of  
| nil => **assert (false)**  
| cons => a.cons;

# Label Refinement Translation

---

$$\oplus \{\text{cons}: \text{int} \wedge \text{list}\}_a \Leftarrow \oplus \{\text{cons}: \text{int} \wedge \text{list}; \text{nil}: 1\}_b$$

case b of

- | nil => **assert (false)**
- | cons => a.cons;

$$\{\text{int} \wedge \text{list}\}_a \Leftarrow \{\text{int} \wedge \text{list}\}_b$$

# Translation is Transparent

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- Prove that generated monitors are partial identity processes

$$\begin{array}{c} a : A \leftarrow b : B \\ \approx \\ a \leftarrow \boxed{\{A\}_a \Leftarrow \{B\}_b} \leftarrow b \end{array}$$

# Redundant Monitor

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$$\oplus \{\text{cons}: \text{int} \wedge \text{list}; \text{nil}: 1\}_a \Leftarrow \oplus \{\text{cons}: \text{int} \wedge \text{list}\}_b$$

case b of

| cons => a.cons;

$$\{\text{int} \wedge \text{list}\}_a \Leftarrow \{\text{int} \wedge \text{list}\}_b$$

# Safety Theorem

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- Prove that subtype casts do not cause assertion failures

$$\boxed{B \leq A}$$
$$a \leftarrow \{A\}_a \Leftarrow \{B\}_b \leftarrow b$$

# Safety Theorem

---

- Prove that subtype casts do not cause assertion failures

$$a \leftarrow \boxed{\{A\}_a} \overset{B \leq A}{=} \{B\}_b \leftarrow b$$

# Partial Identity Rules

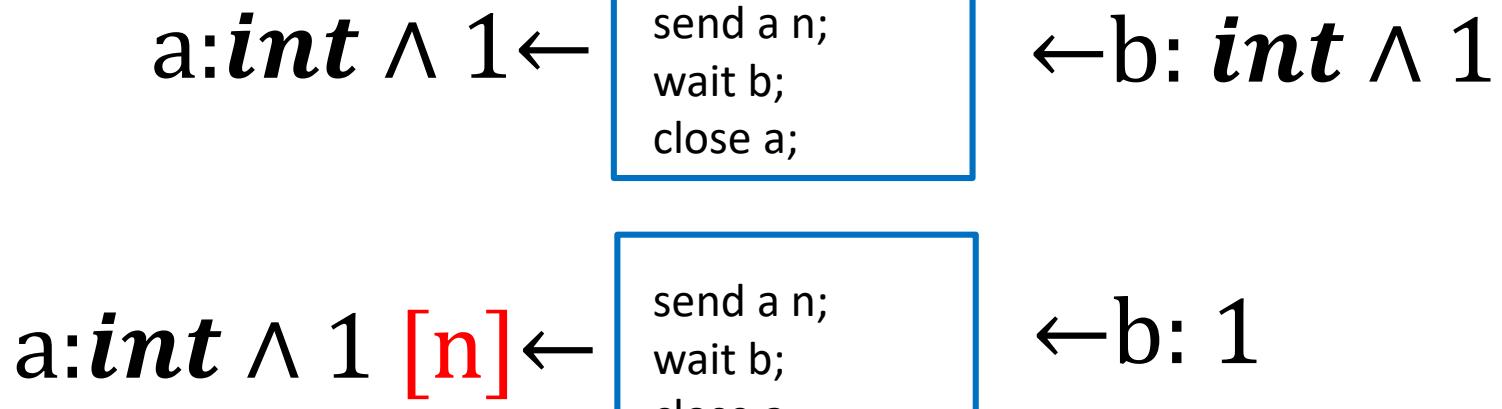
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$a:\textit{int} \wedge 1 \leftarrow \quad \quad \quad \leftarrow b: \textit{int} \wedge 1$

```
n ← recv b;  
send a n;  
wait b;  
close a;
```

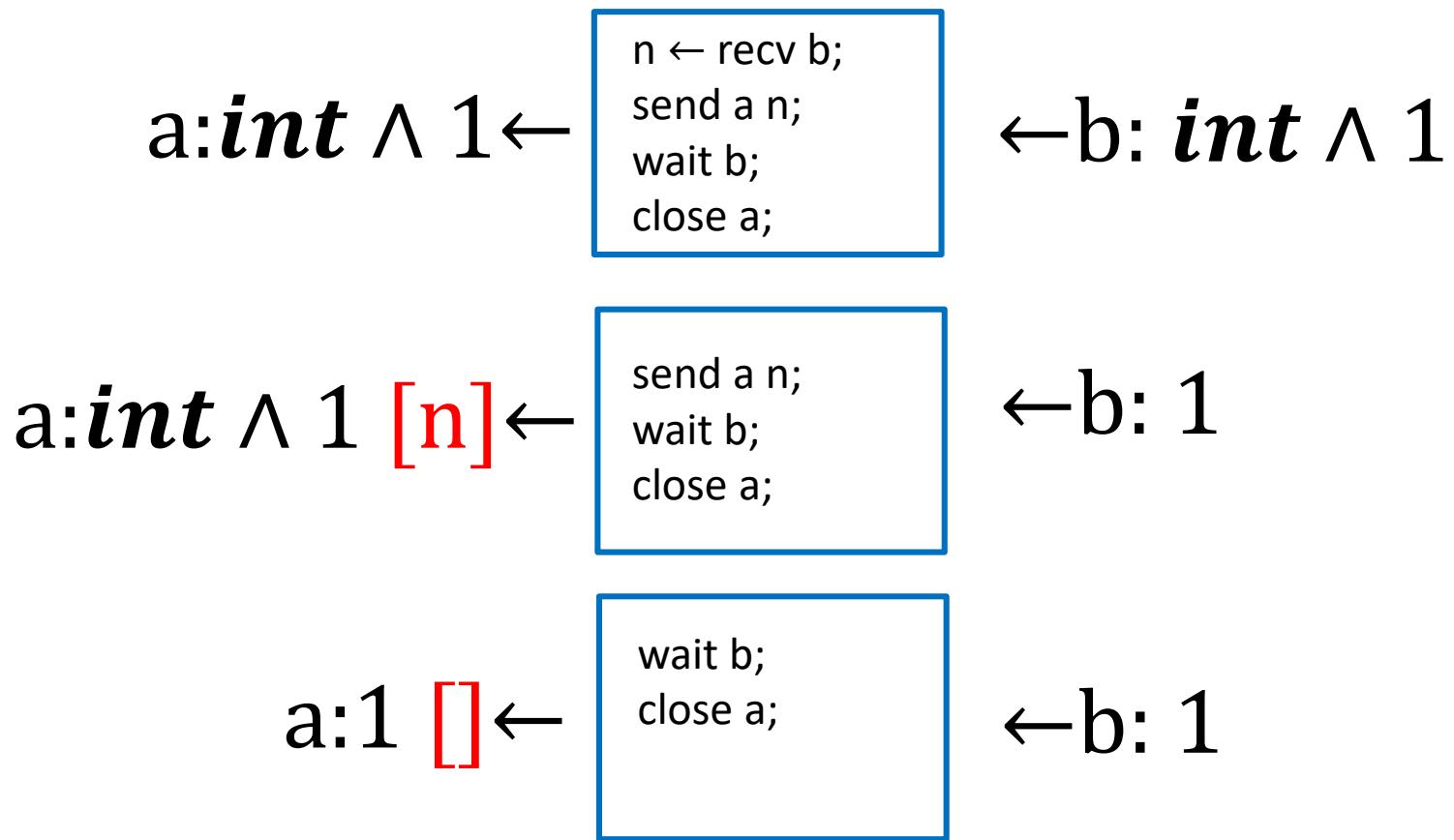
# Partial Identity Rules

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# Partial Identity Rules

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# Partial Identity Criterion

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- Complications occur when monitors spawn other monitors (higher order case)
- Construct a bisimulation between monitoring processes and identity processes showing that every observable message is the same

# Future Work

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- Even more exciting contracts!
  - Contracts which require distributed state (ghost messages), ie permutation checking
  - Noninterference/information flow contracts

# Related Work

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- Recently:
  - Melgratti & Padovani (ICFP 2017)
  - Wuye et al (ICFP 2017)
- Contracts: Findler & Felleisen (2002), Dimoulas et al (2011,2012), Disney et al (2012)

# Takeaway

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Partial identity monitors provide a mechanism to express complex stateful contracts in the same language as the target code